

# Nonlinear Thermal Radiation and Chemical Reaction Effects on MHD 3D Casson Fluid Flow in Porous Medium

C.Sulochana M.K.Kishor Kumar N.Sandeep  
Department of Mathematics, Gulbarga University, Gulbarga-585106, India

## Abstract

In this study, we analyzed the influence of nonlinear thermal radiation and viscous dissipation on three-dimensional MHD Casson fluid flow over a stretching surface in the presence of chemical reaction. The transformed governing equations are solved numerically using Runge-Kutta based shooting technique. The influence of non-dimensional parameters on velocity, temperature and concentration profiles along with the friction factor, local Nusselt and Sherwood numbers are discussed with the help of graphs and tables. It is found that an increase in the nonlinear thermal radiation parameter enhances the temperature profiles of the flow. Chemical reaction parameter have tendency to enhance the mass transfer rate.

**Keywords:** MHD, Casson fluid, Radiation, Chemical Reaction, Dissipation.

## 1. Introduction

The study of Non-Newtonian fluids has attracted much attention because of their extensive variety of applications in engineering and industry especially in extraction of crude oil from petroleum products. In this category of non-Newtonian fluids Casson fluid has distinct features. This model is cast off by fuel engineers in the description for adhesive slurry and is improved for forecasting high shear rate viscosities when only low and transitional shear rate data are accessible. The Magnetohydrodynamic boundary layer flow and heat transfer of a fluid with variable viscosity through a porous medium towards a stretching sheet by taking in to effects of viscous dissipation in presence of heat sources was analyzed by Dessie and Kishan (2014). The Magnetohydrodynamic boundary layer flow of a Casson fluid over an exponentially shrinking sheet has been investigated by Nadeem et al. (2012). The Magnetohydrodynamic Casson fluid flow in porous medium through linear stretching sheet was discussed by Nadeem et al. (2013). The influence of aligned magnetic field and thermal radiation on the flow of nanofluid passing exponentially stretching sheet in porous medium was investigated by Sulochana et al. (2015).

The study of triple diffusive boundary layer flow of a nanofluid over a nonlinear stretching sheet was studied by Goyal and Rama Bhargava (2014). An unsteady mixed convection boundary layer flow over an impermeable stretching sheet in a porous medium in the presence of chemical reaction was examined by Nayak et al. (2014). MHD Casson fluid flow and heat transfer with second-order slip velocity over a permeable stretching sheet in the presence of internal heat generation/absorption was discussed by Ahmed (2015). The heat transfer characteristics of the flow over a stretching sheet the presence of magneticfield and thermal radiation was analyzed by Anjali Devi and Prakash (2015). The effects of thermal radiation on the flow of an incompressible viscous electrically conducting fluid over an unsteady stretching sheet embedded in a porous medium in the presence of heat source or sink was studied by Santosh et al. (2015). Raju et al. (2015) discussed the effect of aligned magneticfield on the flow of a ferro fluid over a plate. He extended this work by considering the flow over a stretching surface.

The study of heat transfer of a viscous nanofluid over a nonlinearly stretching sheet in the presence of thermal radiation was stated by Hady et al. (2012). The Magnetohydrodynamic boundary surface of a Casson fluid in the presence of nano particles was investigated by Hussain et al. (2015). Mohan Krishna et al. (2013, 2014, 2015) discussed the effect of thermal radiation by considering different types of flows. Ramana Reddy et al. (2014) studied the aligned magneticfield, radiation and chemical reaction effects on unsteady dusty viscous flow. Sandeep et al. (2012-15) presented their valuable contributions to analyze the heat and mass transfer performance of the different types of fluids. Sugunamma and Sandeep (2011) discussed an unsteady hydromagnetic free convection flow of a dissipative and radiating fluid past a vertical plate through porous media.

The main aim of this study is to investigate the influence of nonlinear thermal radiation and viscous dissipation on three-dimensional MHD Casson fluid flow over a stretching surface in the presence of chemical reaction. The transformed governing equations are solved numerically using Runge-Kutta based shooting technique. The influence of non-dimensional parameters on velocity, temperature and concentration profiles along with the friction factor, local Nusselt and Sherwood numbers are discussed with the help of graphs and tables.

## 2. Problem statement

Consider a three-dimensional, steady, incompressible flow of a Casson fluid over a stretching sheet. It is

considered that the sheet is stretched along the  $xy$ -plane while fluid is placed along the  $z$ -axis. Moreover, it is considered that constant magnetic field is applying normal to the fluid flow. The heat transfer process is taken in to account. It is assumed that induced magnetic field is negligible. Here, we assumed that sheet has stretched with the linear velocities (Fig. 1)  $u = ax$  and  $v = by$  along the  $xy$ -plane, respectively, with constants  $a$  and  $b$ . The rheological equation of state for an isotropic flow of a Casson fluid can be expressed as follows:

$$\tau_{ij} = \begin{cases} 2 \left( \mu_B + \frac{p_z}{\sqrt{2\pi}} \right) e_{ij}, & \pi > \pi_c \\ 2 \left( \mu_B + \frac{p_z}{\sqrt{2\pi}} \right) e_{ij}, & \pi < \pi_c \end{cases}$$

In the above equation  $\pi = e_{ij}e_{ij}$  and  $e_{ij}$  denotes  $(i, j)^{th}$  component of the deformation rate,  $\pi$  be the product of the component of deformation rate itself,  $\pi_c$  be critical value of this product based on the non-Newtonian model,  $\mu_B$  be the plastic dynamic viscosity of the Casson fluid and  $p_z$  be the yield stress of the fluid.

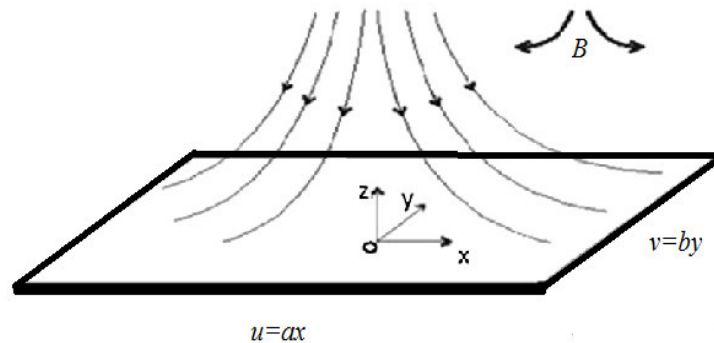


Fig. 1 Physical model and coordinate system

The conservation equation of continuity, momentum and energy equation is as follows:  $\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0$ , (1)

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} = \nu \left( 1 + \frac{1}{\beta} \right) \frac{\partial^2 u}{\partial z^2} - \frac{\sigma B^2}{\rho} u - \frac{\nu}{K_p} u, \quad (2)$$

$$u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} = \nu \left( 1 + \frac{1}{\beta} \right) \frac{\partial^2 v}{\partial z^2} - \frac{\sigma B^2}{\rho} v - \frac{\nu}{K_p} v, \quad (3)$$

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} + w \frac{\partial T}{\partial z} = \frac{k}{\rho c_p} \frac{\partial^2 T}{\partial z^2} + \frac{16\sigma^*}{3\rho c_p k^*} \frac{\partial}{\partial z} \left( T^3 \frac{\partial T}{\partial z} \right) + \frac{\mu}{\rho C_p} \left( 1 + \frac{1}{\beta} \right) \left( \frac{\partial w}{\partial z} \right)^2, \quad (4)$$

$$u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} + w \frac{\partial C}{\partial z} = D_m \frac{\partial^2 C}{\partial z^2} - k_l (C - C_\infty), \quad (5)$$

Where  $u, v$  and  $w$  are the velocity components in the  $x, y$  and  $z$ -direction, respectively,  $\beta = \mu_B \sqrt{2\pi_c} / p_z$  is the Casson fluid parameter,  $B$  is the magnetic induction,  $T$  is the temperature,  $\nu$  be the viscosity,  $K_p$  is the permeability,  $\rho$  is the density of the fluid,  $k$  is the thermal conductivity,  $D_m$  is the mass diffusivity,  $k_l$  is the chemical reaction and  $c_p$  is specific heat capacitance.

The associated boundary conditions of Eqn. (2)-(5) are as follows:

$$u = U_w(x) = ax, \quad v = V_w(x) = by, \quad w = 0$$

$$-k \frac{\partial T}{\partial z} = h_f(T_f - T), -D_m \frac{\partial C}{\partial z} = h_s(C_f - C) \text{ at } z = 0 \quad (6)$$

$$u \rightarrow 0, v \rightarrow 0, T \rightarrow T_\infty, C \rightarrow C_\infty \text{ as } z \rightarrow \infty \quad (7)$$

In the above expression,  $U_w$  and  $V_w$  are stretching velocities in the  $x$  and  $y$  directions, respectively.  $h_f$  is the convective heat transfer coefficient and  $T_f$  is the convective fluid temperature below the sheet,  $h_s$  is the mass transfer coefficient and  $C_f$  is the fluid concentration below the sheet.

Introducing the following similarity transformations

$$u = axf'(\eta), \quad v = byg'(\eta), \quad w = -\sqrt{a/v}(f(\eta) + g(\eta))$$

$$\theta(\eta) = \frac{T - T_\infty}{T_f - T_\infty}, \quad \eta = z\sqrt{a/v}, \quad \phi(\eta) = \left( \frac{c - c_\infty}{c_f - c_\infty} \right) \quad (8)$$

Equation (1) is automatically satisfied by (8) and Equations. (2) - (5) become

$$\left(1 + \frac{1}{\beta}\right) f''' - (f')^2 - (f + cg)f'' - (M + K)f' = 0, \quad (9)$$

$$\left(1 + \frac{1}{\beta}\right) g''' - (g')^2 - (f + cg)g'' - (M + K)g' = 0 \quad (10)$$

$$\left[1 + R(1 + (\theta_w - 1)\theta)^3\right] \theta'' + R\left[3(\theta_w - 1)\theta^2\right] \left[1 + (\theta_w - 1)\theta\right]^2 + Pr Ec (f' + cg')^2 \quad (11)$$

$$\frac{1}{Sc} \phi'' + (f + cg)\phi' - Kr\phi = 0 \quad (12)$$

With the boundary conditions

$$f = 0, \quad g = 0, \quad f' = 1, \quad g' = c, \quad (13)$$

$$\theta' = -Bi_1(1 - \theta(0)), \quad \phi' = -Bi_2(1 - \phi(0))$$

$$f' = 0, \quad g' \rightarrow 0, \quad \theta \rightarrow 0, \quad \phi \rightarrow 0, \text{ as } \eta \rightarrow \infty \quad (14)$$

In the above expression  $M = \frac{\sigma B_0^2}{\rho a}$  is a magnetic parameter,  $K = \frac{v}{aK_p}$  is the porosity parameter,

$Pr = \frac{\rho c_p}{k}$  is Prandtl number,  $R = \frac{16\sigma^* T_\infty^3}{3kk^*}$  is the radiation parameter,

$Bi_1 = \frac{h_f}{k} \left(\sqrt{v/a}\right)$ ,  $Bi_2 = \frac{h_s}{D_m} \left(\sqrt{v/a}\right)$  are the Biot numbers and  $c = b/a$  is the stretching parameter and

Schmidt number  $Sc = \frac{D_m}{v}$  and Eckert number  $Ec = \frac{a}{T_\infty Cp(\theta_w - 1)}$ .

### 3. Skin friction and local Nusselt number

Expression for skin friction coefficient  $C_f$  on the surface along the  $x$  and  $y$  -directions, which are denoted by  $C_{fx}$  and  $C_{fy}$ , respectively are as follows:

$$C_{fx} = \frac{\tau_{wx}}{\rho u_w^2}, \quad C_{fy} = \frac{\tau_{wy}}{\rho u_w^2} \quad (15)$$

Where  $\tau_{wx}$ , and  $\tau_{wy}$  are the wall shear stress along  $x$  and  $y$  -directions, respectively.

$$Re_x^{1/2} C_{fx} = \left(1 + \frac{1}{\beta}\right) f''(0), Re_x^{1/2} C_{fy} = \left(1 + \frac{1}{\beta}\right) g''(0) \quad (16)$$

where  $Re_x = u_x(x) x / \nu$  is the local Reynolds number which depends on the stretching velocity  $u_w(x)$ .

The local Nusselt and Sherwood numbers in non-dimensional form are given by

$$Re_x^{-1/2} Nu = -\theta'(0), Re_x^{-1/2} Sh = -\phi'(0), \quad (17)$$

#### 4. Results and discussion

The system of equations (9) to (12) subjected to the boundary conditions (13) and (14) solved numerically. The study is conducted on Newtonian and Non-Newtonian fluids to illustrate the effects of different governing parameters like, the Magnetic field parameter  $M$ , Radiation parameter  $R$ , wall temperature  $\theta_w$ , Stretching parameter  $c$ , Chemical reaction  $Kr$ , Biot number  $Bi_1, Bi_2$  and Schmidt number  $Sc$  on velocity, temperature and concentration profiles of the flow. For numerical results we considered  $Sc = 2, M = 1, Bi_1 = 0.8, K = c = R = Kr = Sr = Bi_2 = 0.5, Pr = 3, Ec = 0.2, \theta_w = 1.1$ , these values are kept as common in entire study except the varied values as displayed in the respective graphs and tables.

Figs. 2-5 show the effect of magnetic field parameter on velocity, temperature and concentration profiles of the flow. It can be seen that the result is true since the velocity decreases with increase in magnetic parameter  $M$ . It is evident that an increase in the magnetic field parameter depreciates the velocity and enhances the temperature and concentration profiles of the flow. It is due to the fact that the increasing magnetic field parameter improves the opposite force to the flow of direction which is called Lorentz force. This shows that the Lorentz force slows down the motion of electrically conducting fluid.

Figs. 5 and 6 show that an increase in the radiation parameter and temperature parameter enhances the temperature profiles of the flow. This is due to the fact that a rise in the radiation parameter releases the heat energy to the flow. This agrees with the general physical behaviour of the radiation parameter. Figs. 8 -11 depict the effect of stretching ratio parameter on velocity, temperature and concentration profiles of the flow. It is clear that an increase in the stretching ratio parameter declines  $f'(\eta)$ , temperature and concentration profiles. But it showed reverse action in the velocity profiles  $g'(\eta)$ .

Fig. 12 illustrates the effects of chemical reaction parameter on the concentration profile of the flow. It is clear that an increase in the chemical reaction parameter declines the concentration profile of the flow. Figs. 13 and 14 show the effect of Biot numbers on temperature and concentration profiles. It indicates that the increase in Biot number  $Bi_1$  increases the temperature profiles and an increase in the Biot number  $Bi_2$  enhances the concentration profiles of the flow. Physically, the Biot number is expressed as the convection at the surface of the body to the conduction within the surface of the body. When thermal gradient is applied on the surface, the ratio governing the temperature inside the body varies significantly, while the body heats or cools over a time.

Table 1 shows the variation in friction factors, local Nusselt and Sherwood numbers for different values of non-dimensional parameters. It is evident that magnetic field parameter have tendency to reduce the friction factors along with heat and mass transfer rate. Chemical reaction parameter have tendency to enhance the mass transfer rate. Radiation parameter declines the heat transfer rate and Biot numbers are shown mixed response in heat and mass transfer performance.

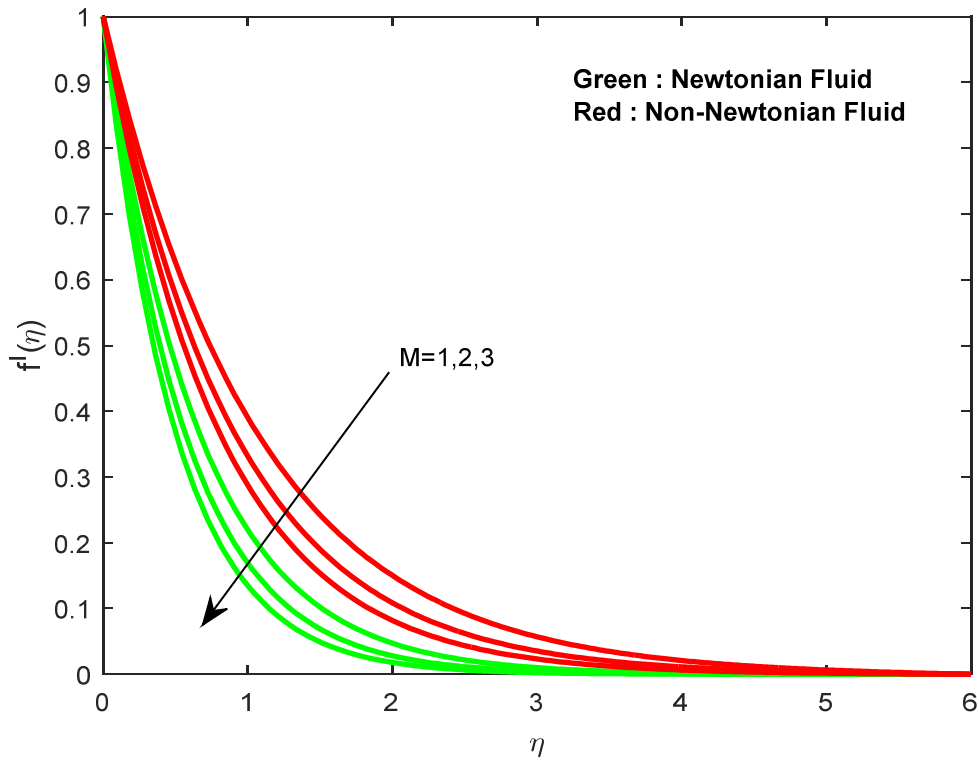


Fig.2 Velocity profiles for various values of Magnetic parameter M

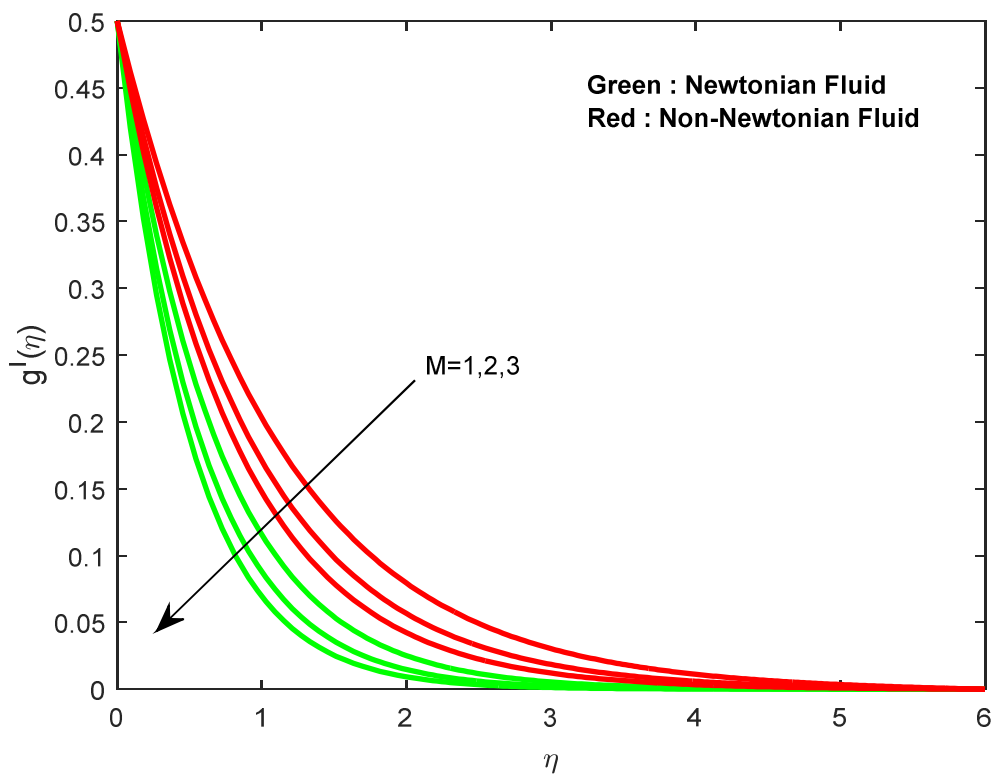


Fig.3 Velocity profiles for various values of Magnetic parameter M

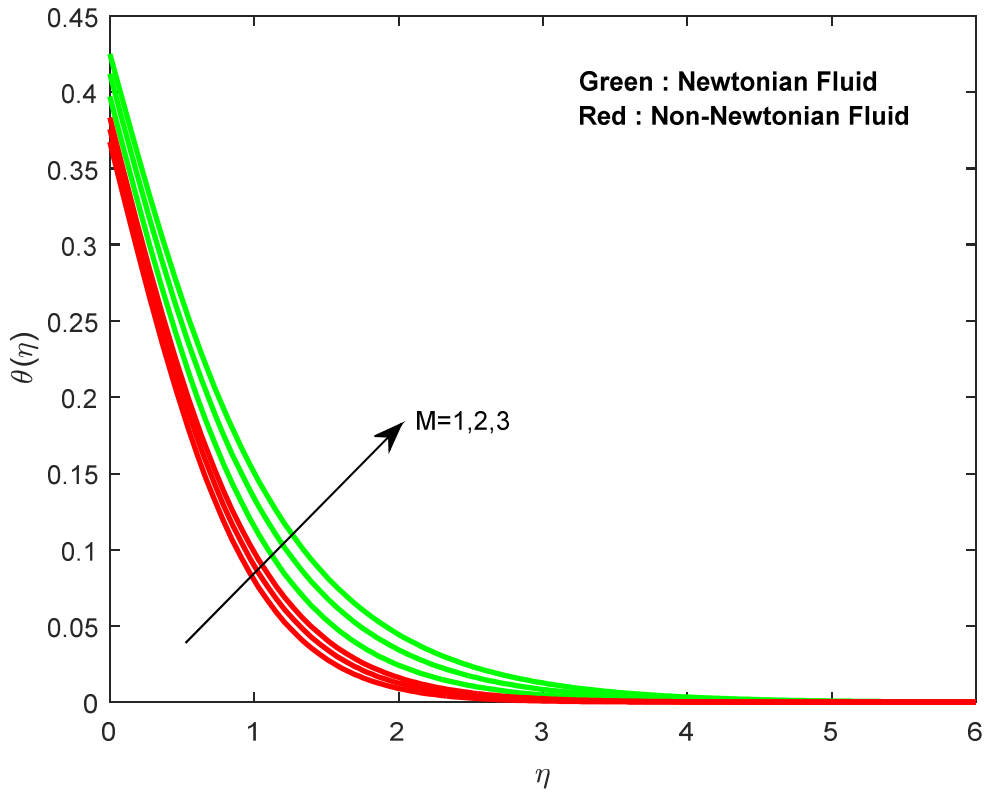


Fig.4 Temperature profiles for various values of Magnetic parameter M

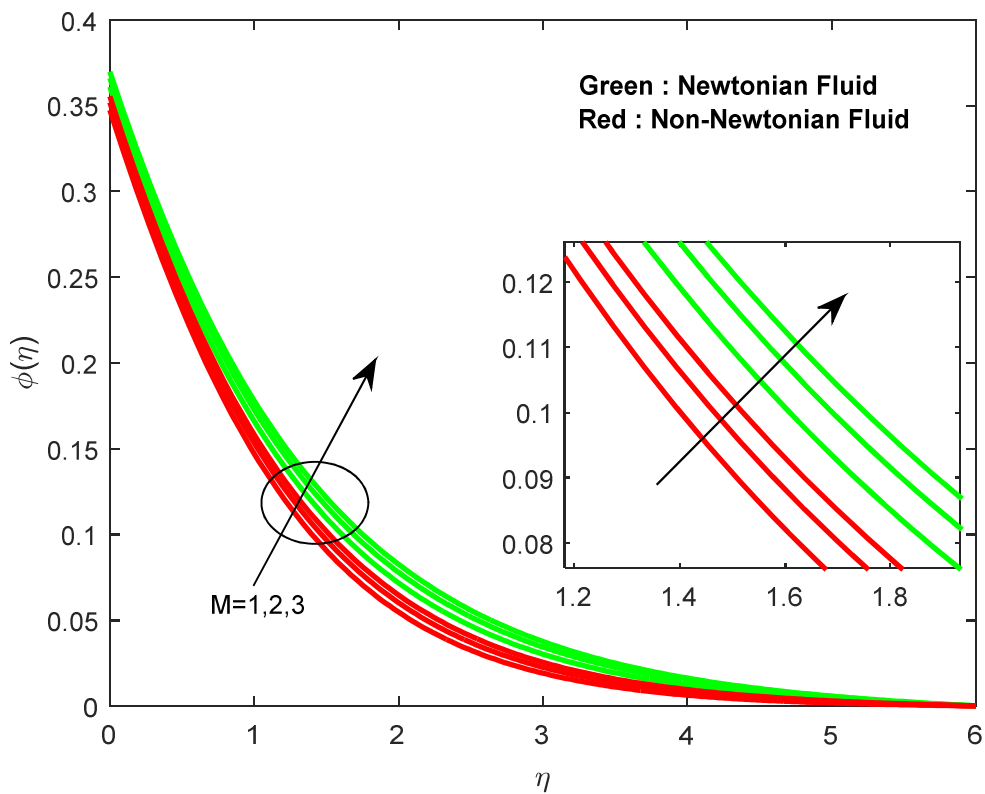


Fig.5 Concentration profiles for varies values of Magnetic parameter M

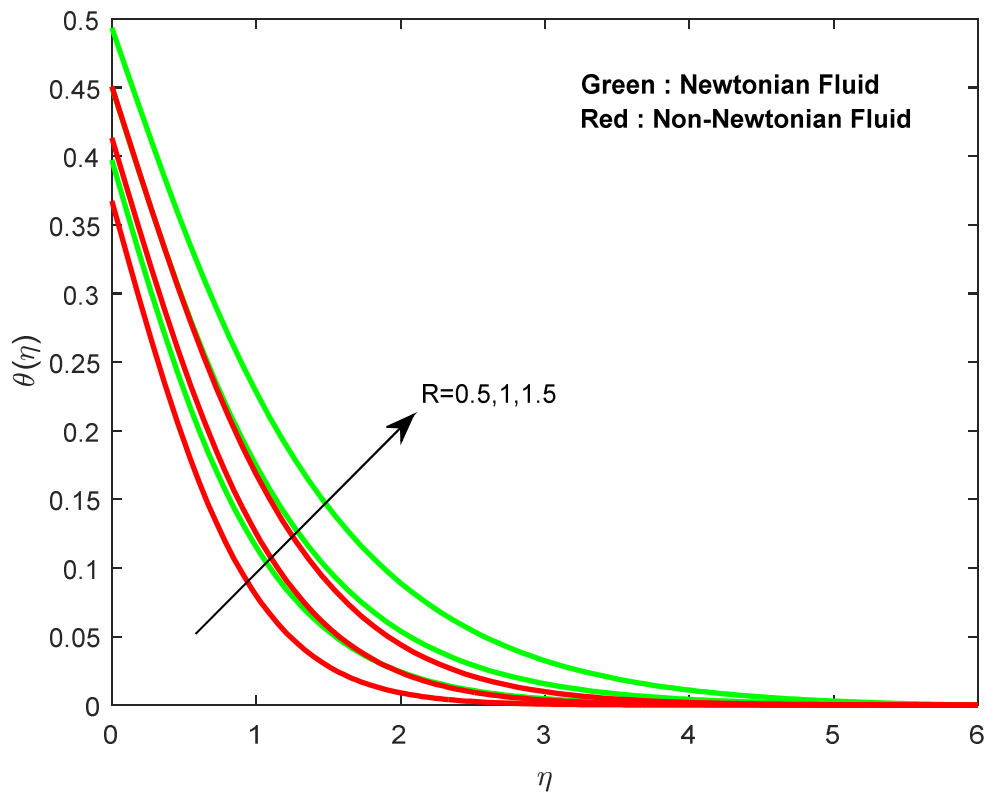


Fig.6 Temperature profiles for various values of Radiation parameter R

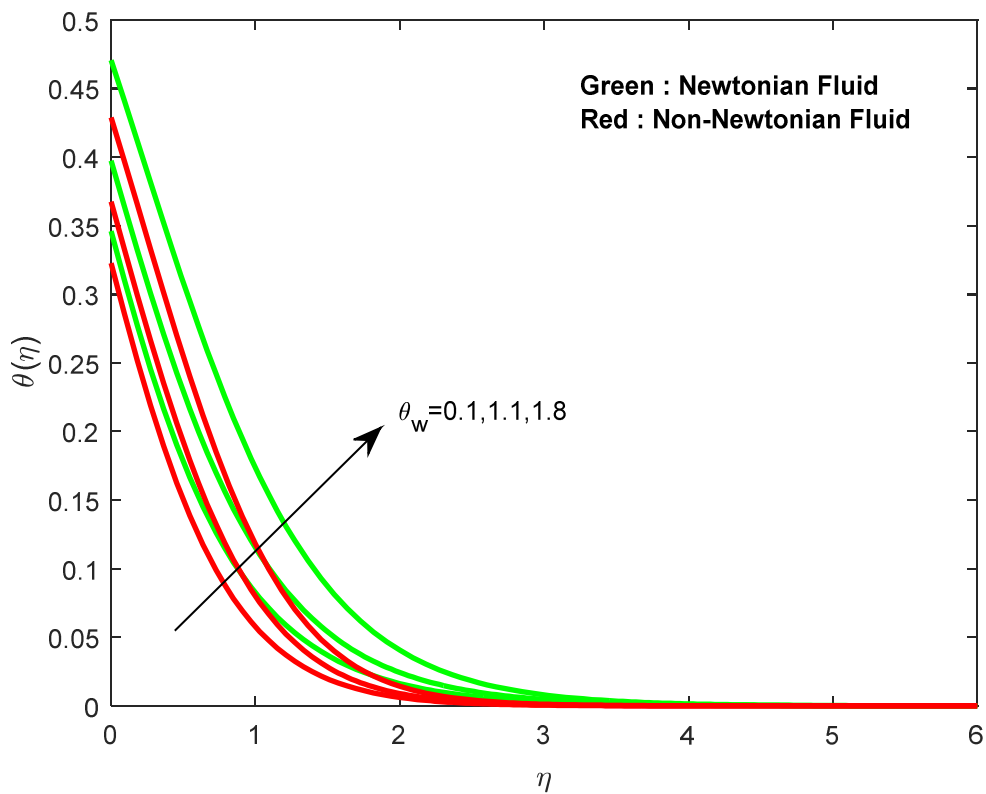


Fig.7 Temperature profiles for various values of wall temperature  $\theta_w$

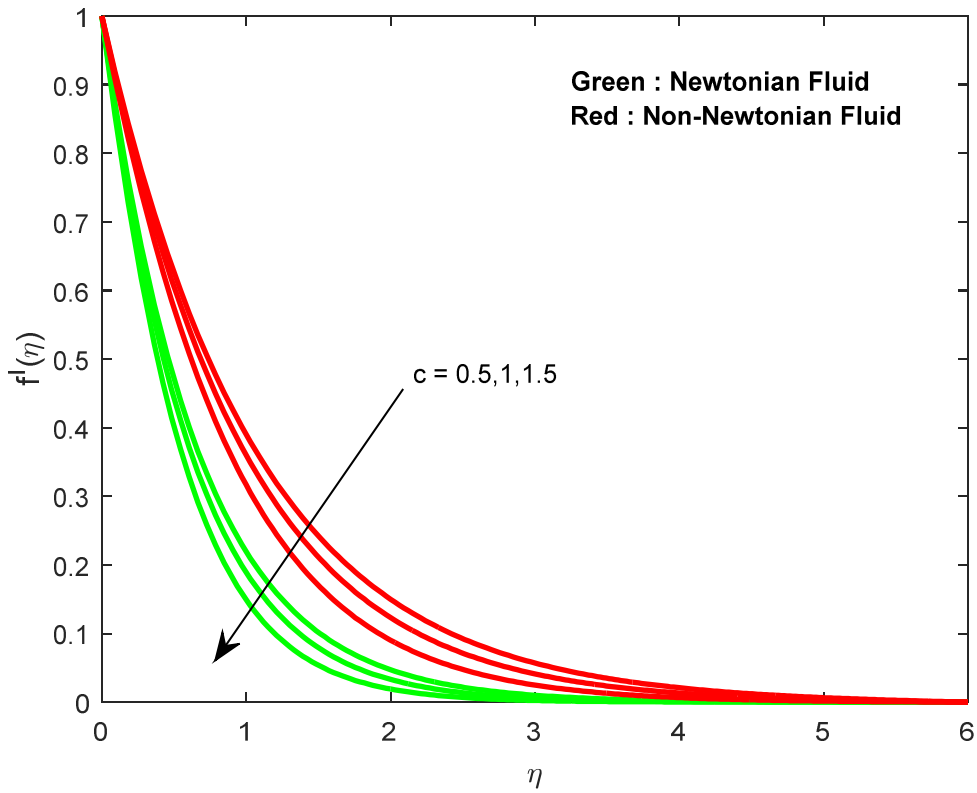


Fig.8 Velocity profile for various values of Stretching parameter c

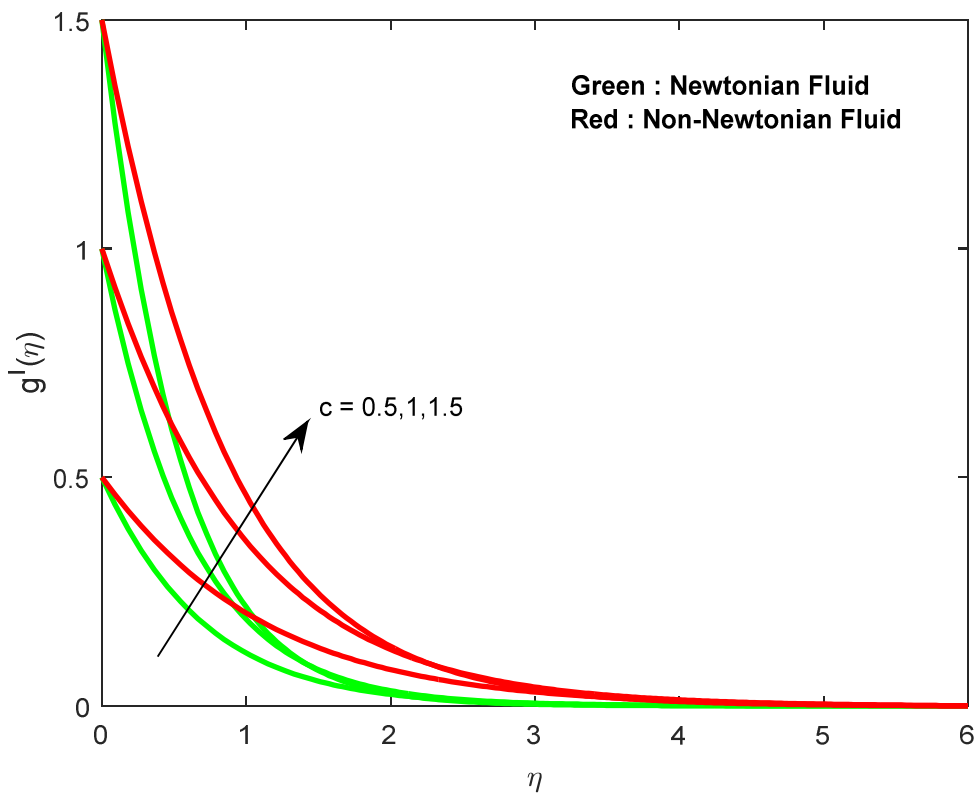


Fig.9 Velocity profiles for varies values of stretching parameter c



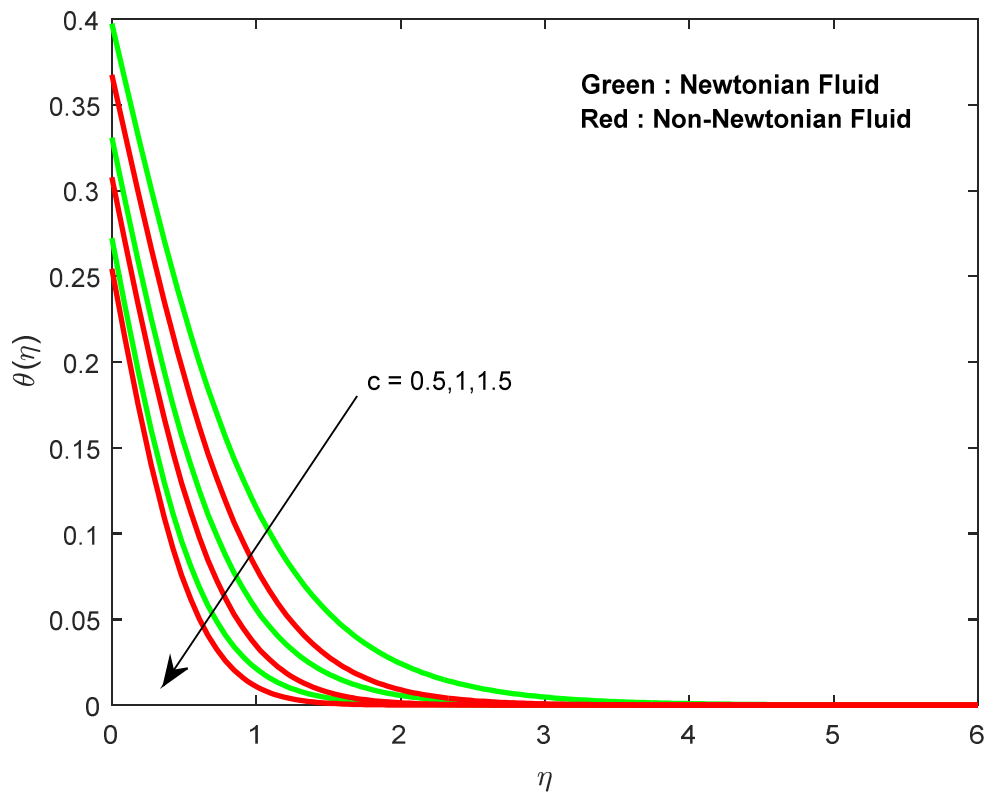


Fig.10 Temperature profiles for various values of Stretching parameter c

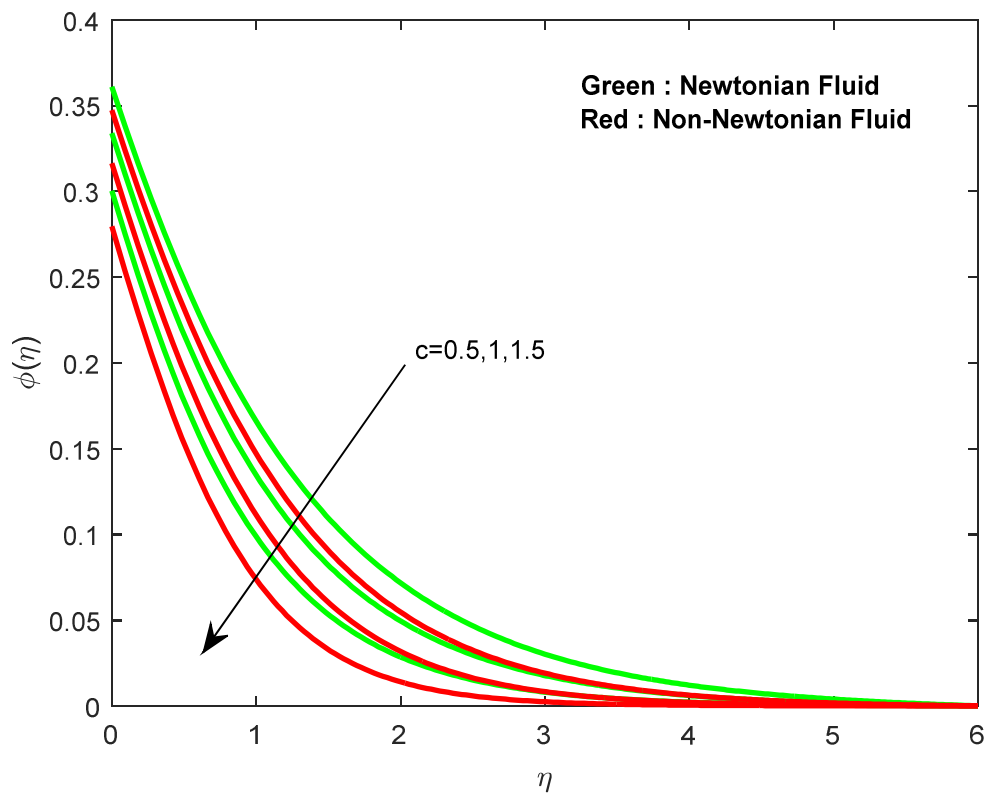


Fig.11 Concentration profiles for varies values of stretching parameter c

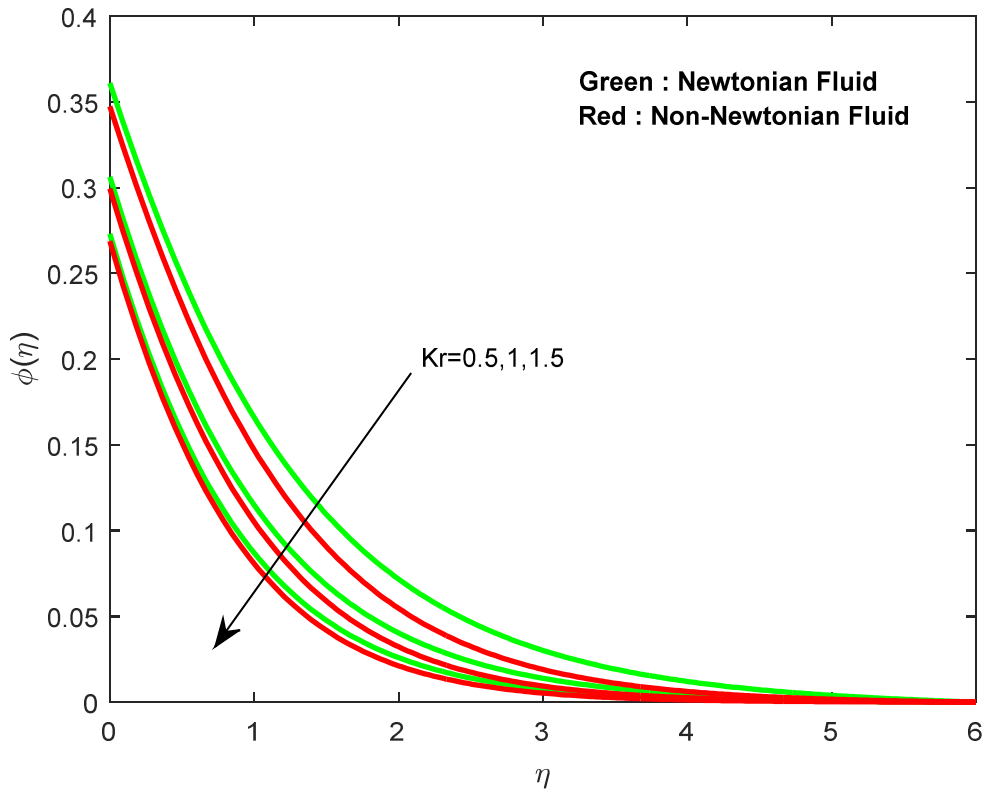


Fig.12 Concentration profiles for varies values of Chemical reaction  $Kr$

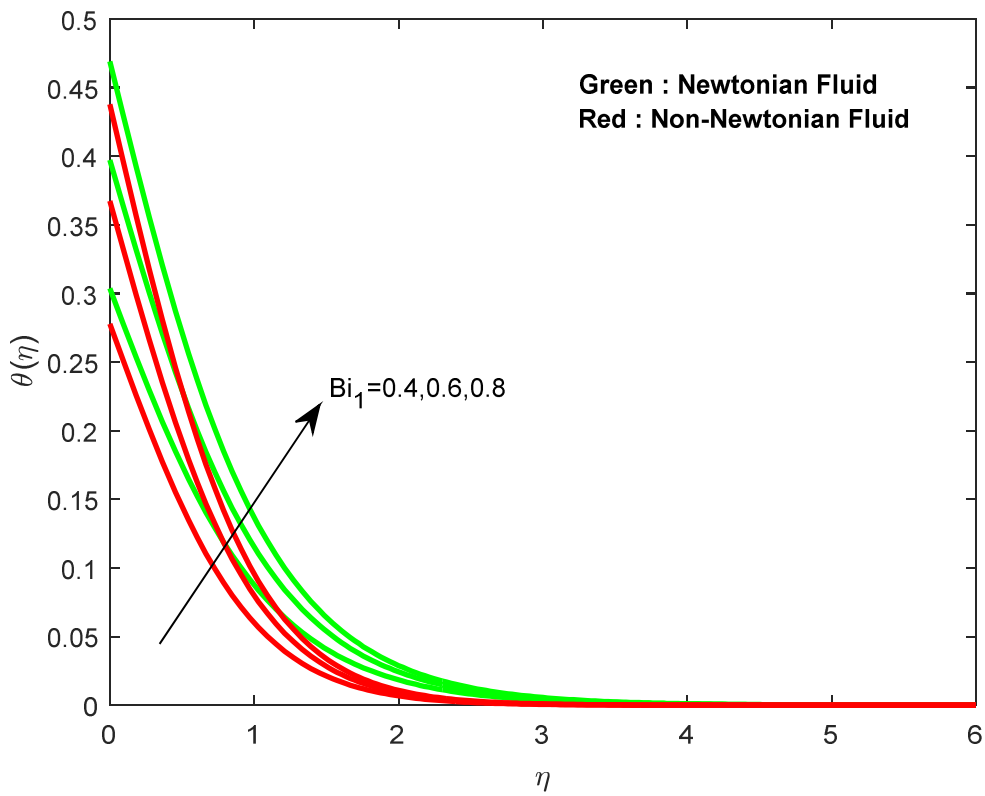


Fig.13 Temperature profiles for various values of Biot number  $Bi_1$

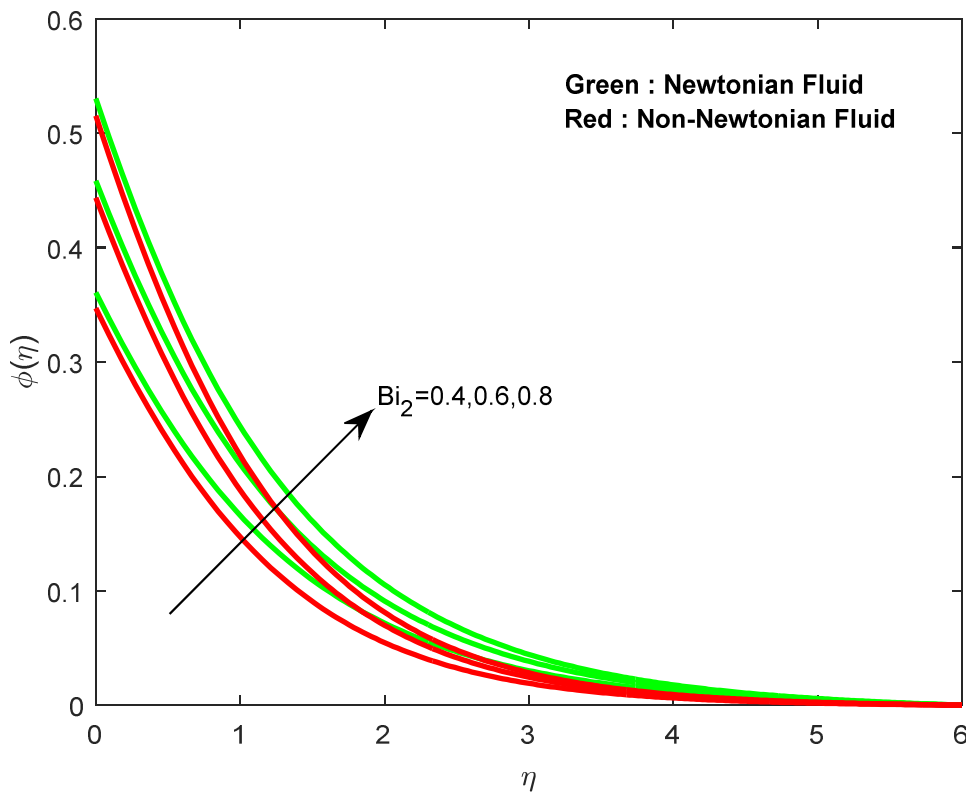


Fig.14 Concentration profiles for varies values of Biot number  $Bi_2$

**Table 1** Variation in  $f''(0)$ ,  $g''(0)$ ,  $-\theta'(0)$  and  $-\phi'(0)$  for Casson fluid at different non dimensional parameters

M	R	c	Kr	$Bi_1$	$Bi_2$	$f''(0)$	$g''(0)$	$-\theta'(0)$	$-\phi'(0)$
1						-0.928995	-0.433610	0.379430	0.261061
2						-1.093475	-0.520730	0.374424	0.259277
3						-1.236412	-0.595323	0.369931	0.257860
	0.5					-0.928995	-0.433610	0.379430	0.261061
	1					-0.928995	-0.433610	0.351900	0.261061
	1.5					-0.928995	-0.433610	0.329343	0.261061
		0.5				-0.928995	-0.433610	0.379430	0.261061
		1				-0.975414	-0.975414	0.415254	0.273461
		1.5				-1.049260	-1.650940	0.447380	0.288164
			0.5			-0.928995	-0.433610	0.379430	0.261061
			1			-0.928995	-0.433610	0.379430	0.280264
			1.5			-0.928995	-0.433610	0.379430	0.292504
				0.4		-0.928995	-0.433610	0.288819	0.261061
				0.6		-0.928995	-0.433610	0.379430	0.261061
				0.8		-0.928995	-0.433610	0.449634	0.261061
					0.4	-0.928995	-0.433610	0.379430	0.261061
					0.6	-0.928995	-0.433610	0.379430	0.333645
					0.8	-0.928995	-0.433610	0.379430	0.387518

### 5. Conclusions

This study presents a numerical solution to investigate the influence of nonlinear thermal radiation and viscous dissipation on three-dimensional MHD Casson fluid flow over a stretching surface in the presence of chemical reaction. The transformed governing equations are solved numerically using Runge-Kutta based shooting technique. The influence of non-dimensional parameters on velocity, temperature and concentration profiles

along with the friction factor, local Nusselt and Sherwood numbers are discussed with the help of graphs and tables. The conclusions of the present study are as follows:

- A raise in magnetic field parameter decreases the friction factor.
- A raise in the stretching ratio parameter enhances the heat and mass transfer rate.
- An increase in the chemical reaction parameter enhances the mass transfer rate.
- An enhancement in radiation parameter enhances the thermal boundary layer thickness, so the temperature profile increases.

## References

- Ahmed, M.M. (2015). MHD viscous Casson fluid flow and heat transfer with second-order slip velocity and thermal slip over a permeable stretching sheet in the presence of internal heat generation/absorption and thermal radiation, *The European Physical Journal Plus*, 130(81), 1-17.
- Anjali Devi, S.P. and Prakash, P. (2015). Thermal radiation effects on hydromagnetic flow over a slandering stretching sheet, *The Journal Brazilian Society of Mechanical Science and Engineering*, 1-9.
- Dessie, H and Naikoti Kishan. (2014). MHD effects on heat transfer over stretching sheet embedded in porous medium with variable viscosity, viscous dissipation and heat Source/Sink, *Ain Shams Engineering Journal*, 5, 967-977.
- Hussain, T., Shehzad, S.A., Alsaedi, A., Hayat, T and Ramzan, M. (2015). Flow of Casson nanofluid with viscous dissipation and convective conditions, *Journal Central South University*, 22, 1132-1140.
- Goyal, M. and Rama Bhargava. (2014). Numerical study of thermodiffusion effects on boundary layer flow of nanofluids over a power law stretching sheet, *Springer-Verlag Berlin Heidelberg*, 17, 591-604.
- Mohan Krishna P, Sugunamma V and Sandeep N (2013). Magnetic field and chemical reaction effects on convective flow of a dusty viscous fluid, *Communications in Applied Sciences*. 1, 161-187.
- Mohan Krishna P, Sugunamma V, Sandeep N (2014). Radiation and magnetic field effects on unsteady natural convection flow of a nanofluid past an infinite vertical plate with heat source, *Chemical and Process Engineering Research*, Vol 25, pp39-52.
- Mohan Krishna P., N.Sandeep, V.Sugunamma. (2015) Effects of radiation and chemical reaction on MHD convective flow over a permeable stretching surface with suction and heat generation. *Walaliak Journal of Science and Technology*, 12(9), 831-847.
- Nadeem, S., Rizwan UI Haq., Norean Sher Akbar and Khan, Z.H. (2013). MHD three-dimensional Casson fluid flow past a porous linearly stretching sheet, *Alexandria Engineering Journal*, 52, 577-582.
- Nadeem, S., Rizwan UI Haq., and Lee, C. (2012). MHD flow of a Casson fluid over an exponentially shrinking sheet, *Scientia Iranica*, 19(6), 1550-1553.
- Nayak, A., Panda, S and Phukan, D.K. (2014). Soret and Dufour effects on mixed convection unsteady MHD boundary layer flow over stretching sheet in porous medium with chemically reactive species, *Applied Mathematics and Mechanics-England Edition*, 35(7), 849-862.
- Raju C.S. K., N. Sandeep, C. Sulochana, V. Sugunamma, (2015a). Effects of aligned magnetic field and radiation on the flow of ferrofluids over a flat plate with non-uniform heat source/sink. *Internat. J. Sci. Eng.*, 8(2), 151-158.
- Raju C. S. K., N. Sandeep, C. Sulochana, V. Sugunamma, M. Jayachandra Babu, (2015b). Radiation, inclined magnetic field and cross-diffusion effects on flow over a stretching surface. *JNNMS* 34, 169-180.
- Ramana Reddy, J.V., Sugunamma, V., Mohan Krishna, P., Sandeep, N. (2014). Aligned magnetic field, Radiation and chemical reaction effects on unsteady dusty viscous flow with heat generation/absorption, *Chemical and process eng. Research*, 27, 37- 53.
- Sandeep N, Reddy A.V.B, Sugunamma V, (2012). Effect of radiation and chemical reaction on transient MHD free convective flow over a vertical plate through porous media. *Chemical and process engineering research*. 2, 1-9.
- Sandeep, N., Sugunamma, V., Mohankrishna, P. (2013). Effects of radiation on an unsteady natural convective flow of a EG-Nimonic 80a nanofluid past an infinite vertical plate. *Advances in Physics Theories and Applications*. 23, 36-43.
- Sandeep N., V.Sugunamma (2014). Radiation and inclined magnetic field effects on unsteady MHD convective flow past an impulsively moving vertical plate in a porous medium. *Journal of Applied and Fluid Mechanics* 7(2), 275-286.
- Sandeep N, C. Sulochana, (2015). Dual solutions of radiative MHD nanofluid flow over an exponentially stretching sheet with heat generation/absorption. *Appl Nanosci* doi 10.1007/s13204-015-0420-z.
- Sandeep N., C.Sulochana (2015). MHD flow of a dusty nanofluid over a stretching surface with volume fraction of dust particles. *Ain Shams Engineering Journal* (Press)
- Santosh Chaudhary., Mohan Kumar Chaudhary and Ritu Sharma. (2015). Effects of thermal radiation on hydromagnetic flow over an unsteady stretching sheet embedded in a porous medium in the presence

- of heat sources or sink, *Springer Science+Business Media Dordrecht*, 50, 1977-1987.
- Sugunamma, V. and Sandeep, N. (2011) .Unsteady hydromagnetic free convection flow of a dissipative and radiating fluid past a vertical plate through porous media with constant heat flux. *International journal of mathematics and computer applications research*. 1, 37-50.
- Sulochana C., N. Sandeep (2015), Stagnation point flow and heat transfer behavior of Cu- water nanofluid towards horizontal and exponentially stretching/shrinking cylinders. *Appl .Nanosci*; doi 10.1007/s13204-015-0451-5.
- Sulochana, M., M.K.Kishore Kumar, N.Sandeep (2015). Influence of aligned magnetic field on the flow through vertical surface in porous medium with heat source. *Advances in Physics Theories and Applications* 42, 33-45.

The IISTE is a pioneer in the Open-Access hosting service and academic event management. The aim of the firm is Accelerating Global Knowledge Sharing.

More information about the firm can be found on the homepage:

<http://www.iiste.org>

### CALL FOR JOURNAL PAPERS

There are more than 30 peer-reviewed academic journals hosted under the hosting platform.

**Prospective authors of journals can find the submission instruction on the following page:** <http://www.iiste.org/journals/> All the journals articles are available online to the readers all over the world without financial, legal, or technical barriers other than those inseparable from gaining access to the internet itself. Paper version of the journals is also available upon request of readers and authors.

### MORE RESOURCES

Book publication information: <http://www.iiste.org/book/>

Academic conference: <http://www.iiste.org/conference/upcoming-conferences-call-for-paper/>

### IISTE Knowledge Sharing Partners

EBSCO, Index Copernicus, Ulrich's Periodicals Directory, JournalTOCS, PKP Open Archives Harvester, Bielefeld Academic Search Engine, Elektronische Zeitschriftenbibliothek EZB, Open J-Gate, OCLC WorldCat, Universe Digital Library, NewJour, Google Scholar

