

Mhd Stagnation Point Flow of a Jeffrey Fluid Over a Stretching/Shrinking Sheet through Porous Medium

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Abstract

In this analysis the MHD stagnation point flow of Jeffrey fluid over a stretching/shrinking sheet through porous medium is studied. The governing partial differential equations are transformed into nonlinear ordinary differential equation using the similarity transformations and are solved shooting technique. The effects of governing parameters on the velocity, the temperature and the concentration while the skin friction coefficients, the rate of heat transfer are studied graphically.

Keywords: MHD; Jeffrey fluid, stretching/shrinking sheet, Porous medium.

INTRODUCTION

Many fluids such as a blood, dyes, ketchup, shampoo, clay cooling, mud, polymer melts certain oils and greases etc., have complicated relations between stress and strain. Such fluids don't obey the Newton's law of viscosity and are usually called non-Newtonian fluids. The study of non-Newtonian fluids has gained interest because of their numerous technological applications, including manufacturing of plastic sheets, performance of lubricants, transpiration cooling, thermal oil recovery and movement of biological fluids. The mass transfer analysis in boundary layer flow is of great importance in extending the theory of separation processes and chemical kinetics. In particular, the boundary layer flow of non-Newtonian fluids due to a stretching surface has gained much importance in many engineering and industrial applications that include both metal and polymer sheet. The reason for such acceleration interest is due to its wide occurrence in various applications such as biological sciences, geophysics, chemical and petroleum industries etc. In view of their differences with Newtonian fluids, several models of non-Newtonian fluids have been proposed by various researchers. Among these, the Jeffrey model is a rate type of non-Newtonian fluid which is capable of describing the characteristic of relaxation and retardation times.

Flow in the boundary layer on a continuous solid surface with constant speed was studied by Sakiadis (1961). Due to entrainment of ambient fluid, this boundary layer is different from that in Blasius flow past a flat plate. Erickson, Fan, and Fox (1966) extended this problem to the case where suction or blowing existed at the moving surface. Crane (1970) considered the moving strip whose velocity is proportional to the distance from the slit. These types of flow usually occur during the drawing of plastic films and artificial fibers. The heat and mass transfer on a stretching sheet with suction or blowing was investigated by Gupta and Gupta (1977). They dealt with the isothermal moving plate and obtained temperature and concentration distributions. The problems of the flow through stretching surface have been investigated by Wang (1984). Dutta, Roy, and Gupta (1985) analyzed temperature distribution in the flow over a stretching sheet with uniform heat flux. They have shown that temperature at a point decreases with an increase in the Prandtl number. Recently, Kartini Ahmad, Zahir Hanouf and Anuar Ishak (2016) discussed by Mixed convection Jeffrey fluid flow over an exponentially stretching sheet with magnetohydrodynamic effect. Maria Imtiaz, Tasawar Hayat, Ahmed Alsaedi (2016) studied MHD Convective Flow of Jeffrey Fluid Due to a Curved Stretching Surface with Homogeneous Heterogeneous Reactions. (2016) Effects of diffusion-thermo and thermo-diffusion on two-phase boundary layer flow past a stretching sheet with fluid-particle suspension and chemical reaction, a numerical study by K.L. Krupa Lakshmi, B.J. Gireesha, Rama.S.R. Gorla, B. Mahanthesh.

In fluid dynamics, the stagnation point flow and flow over a stretching surface are important in theoretical and applications point of view. In fluid dynamics, stagnation is a point in a flow field where the local velocity of the fluid is zero. Stagnation points exist at the surface of objects in the flow field, where the fluid is brought to rest by the object. Stagnation flow towards a stretching sheet is investigated by Wang (2008). Mixed convection MHD stagnation point flow on vertical, linearly stretching sheet is explained by Ishak (2007-09). The steady two-dimensional stagnation point flow on a stretching sheet was first discussed by Chaim (1998). Stagnation point flow over a stretching surface is explained by T. R. Mahapatra and A. S. Gupta (2003). Recently I. S. Awaludin, P. D. Weidman and Anuar Ishak, (2016) studied the Stability analysis of stagnation-point flow over a stretching/shrinking sheet. Santosh chaudary and Mohan Kumar choudhary (2016) presented by the Heat and mass transfer by MHD flow near the stagnation point over a stretching /shrinking sheet in a porous medium. G.C. Dash, R.S. Tripathy, M.M. Rashidi, S.R. Mishra (2016) studied the Numerical approach to boundary layer stagnation-point flow past a stretching/shrinking sheet. Mohamed Abd El-Aziz (2016) examined the Dual solutions in hydromagnetic stagnation point flow and heat transfer towards a stretching/shrinking sheet with non-

uniform heat source/sink and variable surface heat flux. Nor Azian Aini Mat, Norihan Md. Arifin, Roslinda Nazar, Norfifah Bachok (2015) investigate the Boundary Layer Stagnation-Point Slip Flow and Heat Transfer towards a Shrinking/Stretching Cylinder over a Permeable Surface. N.F. Fauzi, S. Ahmad, I. Pop (2015) worked on Stagnation point flow and heat transfer over a nonlinear shrinking sheet with slip effects. T.M. Agbaje, S. Mondal, Z.G. Makukula, S.S. Motsa, P. Sibanda (2015) studied a new numerical approach to MHD stagnation point flow and heat transfer towards a stretching sheet. Tasawar Hayat, Muhammad Waqas, Sabir Ali Shehzad, Ahmed Alsaedi (2015) investigated the MHD stagnation point flow of Jeffrey fluid by a radially stretching surface with viscous dissipation and Joule heating. K. Bhattacharyya, (2011) has studied the Dual solution in boundary layer stagnation point flow and mass transfer with chemical reaction past a stretching/shrinking sheet. He has considered the fluid to be electrically non-conducting.

Heat transfer in porous media has received considerable attention and has been the field of a number of investigations during the last two decades. The need for fundamental studies in porous media heat transfer stems from the fact that a better understanding of a host of thermal engineering applications in which porous materials are present is required. Some of examples of thermal engineering disciplines which stand to benefit from a better understanding of heat and fluid flow processes through porous media are geothermal systems, thermal insulations, grain storage, solid matrix heat exchangers, oil extraction and manufacturing numerous products in the chemical industry. The application of electromagnetic fields in controlling the heat transfer as in aerodynamic heating leads to the study of magneto hydrodynamic heat transfer. This MHD heat transfer has gained significance owing to recent advancement of space technology. The MHD heat transfer can be divided in two parts. One contains problems in which the heating is an incidental by product of electromagnetic fields as in MHD generators and pumps etc., and the second consists of problems in which the primary use of electromagnetic fields is to control the heat transfer. Heat transfer in channels partially filled with porous media has gained considerable attention in recent years because of its various applications in contemporary technology. These applications include porous journal bearing, blood flow in lungs or in arteries, nuclear reactors, porous flat plate collectors, packed bed thermal storage solidification of concentrated alloys, fibrous and granular insulation, grain storage and drying, paper drying, and food storage. Besides the use of porous substrates to improve heat transfer in channels, which is considered as porous layers, finds applications in heat exchangers, electronic cooling, heat pipes, filtration and chemical reactors etc. In these applications engineers avoid filling entire channel with a solid matrix to reduce the pressure drop. Recently, M. Eswara Rao and S. Sreenadh (2017) studied the MHD Boundary Layer Flow of Jeffrey Fluid over a Stretching/Shrinking Sheet through Porous Medium. N. Vishnu Ganesh, A.K Abdul Hakeem, B. Ganga (2016) analyzed the Darcy-Forchheimer flow of hydromagnetic nanofluid over a stretching/shrinking sheet in a thermally stratified porous medium with second order slip, viscous and Ohmic dissipations effects. S Baag, S.R. Mishra, G.C. Dash, M.R. Acharya (2016) Entropy generation analysis for viscoelastic MHD flow over a stretching sheet embedded in a porous medium. Hayat T, Awais M, Imtiaz (2016) studied the Heat Source/Sink in a Magneto-Hydrodynamic non-Newtonian Fluid Flow in a Porous Medium: Dual Solutions. Vajravelu, K., S. Sreenadh, et al. (2016) discussed the effect of heat transfer on the nonlinear peristaltic transport of a Jeffrey fluid through a finite vertical porous channel. Azhar Ali, H. Zaman, M. Z. Abidin, Naeemullah, S. I. A. Shah (2015) worked on the Analytic Solution for Fluid Flow over an Exponentially Stretching Porous Sheet with Surface Heat Flux in Porous Medium by Means of Homotopy Analysis Method. Ruchika Dhanai, Puneet Rana, Lokendra Kumar (2015) studied the Multiple solutions of MHD boundary layer flow and heat transfer behavior of nanofluids induced by a power-law stretching/shrinking permeable sheet with viscous dissipation.

MATHEMATICAL FORMULATION OF THE PROBLEM

A steady two dimensional boundary layer flow of a Newtonian incompressible electrically conducting fluid near a stagnation point over a stretching /shrinking surface placed in the plane $y = 0$ of Cartesian coordinate system in a saturated porous medium. The x -axis is taken along the surface with origin at the stagnation point and y -axis is perpendicular to it. A uniform magnetic field of strength B_0 is assumed to be applied in the positive y -direction normal to the plate. The magnetic Reynolds number of the flow is taken to be small enough, so that induced magnetic field negligible in comparison with applied one.

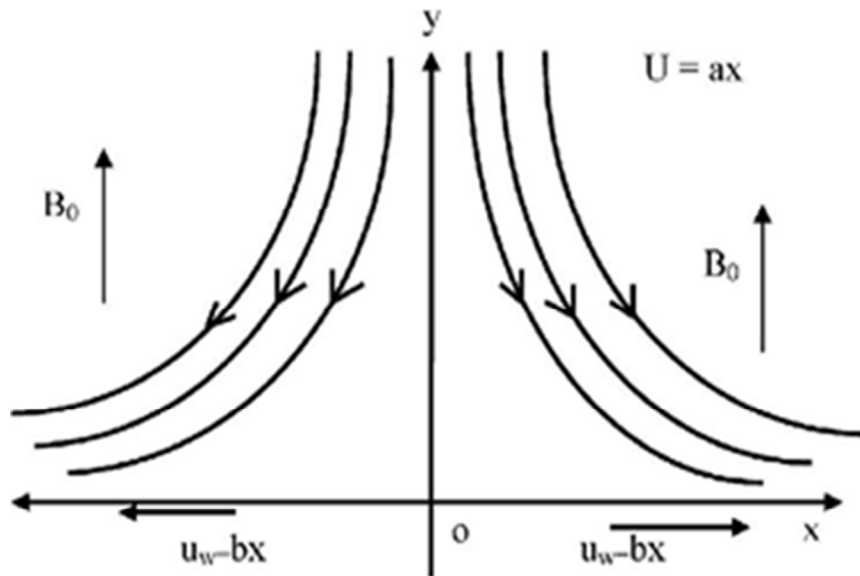


Figure 1. Physical model of the problem

The system of boundary layer equations is of the following is

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \quad (1)$$

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = U_s \frac{\partial U_s}{\partial x} + \frac{v}{1 + \lambda_1} \frac{\partial^2 u}{\partial y^2} - \frac{\sigma B_0^2}{\rho} (u - U) - \frac{v}{k} u \quad (2)$$

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \frac{\kappa}{\rho C_p} \frac{\partial^2 T}{\partial y^2} + \frac{Q}{\rho C_p} (T - T_\infty) \quad (3)$$

$$u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} = D \frac{\partial^2 C}{\partial y^2} - R(C - C_\infty) \quad (4)$$

The boundary conditions are

$$\begin{aligned} u = bx, \quad v = 0, \quad T = T_\omega, \quad C = C_\omega \quad \text{at } y = 0 \\ U \rightarrow U_s(x) = ax, \quad T \rightarrow T_\infty, \quad C \rightarrow C_\infty \quad \text{at } y \rightarrow \infty \end{aligned} \quad (5)$$

SIMILARITY TRANSFORMATIONS

The continuity equation (1) is identically satisfied but introducing a stream function $\psi(x, y)$ such that

$$u = \frac{\partial \psi}{\partial y}, \quad v = -\frac{\partial \psi}{\partial x} \quad (6)$$

The momentum energy and concentration equations (2), (3) and (5) can be transformed into the corresponding ordinary differential equations by introducing the following dimensionless variables are

$$\begin{aligned} \psi(x, y) = \sqrt{av}xf(\eta), \quad \eta = \sqrt{\frac{a}{v}}y \\ \theta(\eta) = \frac{T - T_\infty}{T_\omega - T_\infty}, \quad \phi(\eta) = \frac{C_\omega - C}{C_\omega - C_\infty} \end{aligned} \quad (7)$$

Incorporating equations (6) and (7) into the governing equations (2) and the boundary conditions (5) we finally obtain a system of non-linear ordinary differential equations with appropriate boundary conditions are of following.

$$\left(\frac{1}{1+\lambda_1}\right) f'''' + ff'' - f'^2 - (M + \lambda_2) f' + (1 + M) = 0 \tag{8}$$

$$\theta'' + P_r f \theta' + P_r S \theta = 0 \tag{9}$$

$$\phi'' + S_c f \phi' - S_c \beta \phi = 0 \tag{10}$$

And the boundary conditions are

$$f(0) = 0, f'(0) = b/a, \theta(0) = 1, \phi(0) = 1 \text{ at } \eta = 0$$

$$f'(\infty) \rightarrow 1, \theta(\infty) \rightarrow 0, \phi(\infty) \rightarrow 0 \text{ at } \eta \rightarrow \infty \tag{11}$$

Where primes denote differentiation with respect to η , $M = \sqrt{\frac{\sigma}{\rho b}} B_0$ magnetic parameter, $P_r = \frac{\nu}{\kappa}$ Prandtl number,

$S_c = \frac{\nu}{D}$ Schmidt number, $\lambda_2 = \frac{\nu}{a\kappa}$ porous parameter λ_1 Jeffrey parameter, $S =$ heat source

parameter and $\beta = \frac{R}{a}$ the non-dimensional reaction rate of solutal.

Physical quantities of interest are skin friction coefficient C_f , local rate of heat transfer coefficient N_u and local Sherwood number S_h which are defined as

$$C_f = \frac{\tau_w}{\rho U^2} \sqrt{2}, N_u = \frac{\chi q_w}{\kappa(T_w - T_\infty)}, S_h = \frac{\chi h_m}{D(C_w - C_\infty)} \tag{12}$$

The wall shear stress τ_w the heat flux q_w and mass flux h_m are defined as

$$\tau_w = \frac{\mu}{1+\lambda_1} \left(\frac{\partial u}{\partial y}\right)_{y=0}, h_m = -D \left(\frac{\partial C}{\partial y}\right)_{y=0}, q_w = -\kappa \left(\frac{\partial T}{\partial y}\right)_{y=0} \tag{13}$$

Using the similarity variables equations (6) and (7) we obtain

$$f''(0) = \frac{(1+\lambda_1)}{2} C_f \sqrt{\text{Re}_x}, \frac{Nu}{\sqrt{\text{Re}_x}} = -\theta'(0), \frac{Sh}{\sqrt{\text{Re}_x}} = -\phi'(0) \tag{14}$$

$$\text{Re}_x = \frac{\rho b x^2}{\mu}$$

Where

RESULTS AND DISCUSSION

The present steady on MHD Jeffrey fluid flow over a stretching/shrinking sheet through porous medium is investigated. The governing equations (2), (3) and (4) are solved using Runge-kutta method along with shooting technique. The pertinent governing parameters on velocity $f'(\eta)$, temperature $\theta(\eta)$ and concentration $\phi(\eta)$ through graphs are shown in figures (2)- (4.10) while numerical values of the rate of heat transfer is presented in tabular form.

The velocity $f'(\eta)$ distribution is presented through the Figures 2 and 3 in case of shrinking sheet. The velocity $f'(\eta)$ distribution various values of Jeffrey parameter λ_1 and porous parameter λ_2 are shown in Figure 2. We observed that velocity is decreases with the increasing values of λ_2 for both Newtonian and non-Newtonian case. From Figure 3 shows that the velocity $f'(\eta)$ distribution for different values of the effects of velocity ratio b/a i.e. stretching rate of the bounding surface b and straining rate of the stagnation point flow a

($a > 0$). We observed that the velocity decreases with increasing values of b/a for both cases. The temperature distribution is presented through Figures 4 - 7 in case of shrinking sheet. The temperature $\theta(\eta)$ distribution for various values of the effect of velocity ratio b/a is shown in Figure 4. We observe that the temperature $\theta(\eta)$ increases with increasing b/a for both Newtonian ($\lambda_1 = 0$) and non-Newtonian ($\lambda_1 = 0.5$) cases. Figure 5 exhibit the effect of heat source parameter S on temperature $\theta(\eta)$ distribution. It reveals that the temperature $\theta(\eta)$ increases with increasing S. and a hike in temperature is marked near the plate when the viscosity and conductivity of the fluid the same porosity. From Figure 6 depicts the effect of velocity ratio b/a on temperature gradient $\theta'(\eta)$. It seems that the temperature gradient $\theta'(\eta)$ is increases with b/a up to $\eta = 1.5$ while the opposite behavior at $\eta = 2$ till end of the plate. Figure 7 indicate that temperature $\theta(\eta)$ decreases with increasing Pr for both cases. Figure 8-10 exhibits the profiles related to concentration and its gradient the concentration $\phi(\eta)$ for various values b/a is displayed in Figure 8. It shows that the concentration $\phi(\eta)$ increases with increasing values of b/a for both Newtonian ($\lambda_1 = 0$) and non-Newtonian cases ($\lambda_1 = 0.5$). Figure 9 is devoted to bring out the effect of Schmidt number Sc. It shows that the concentration $\phi(\eta)$ increases with increasing Sc for both cases. Figure 10 exhibit the effect of Schmidt number Sc on concentration gradient $\phi'(\eta)$ increases at the surface with increasing Sc for both cases.

The flow characteristic at the bounding surface are vital in determine the flow stability. Table-1 shows the rate of heat transfer for stretching/shrinking of the plate surface. It is seen from the table the Nusselt Number (Nu) decreases with an increase in the value of Pr in the absence of Jeffrey parameter ($\lambda_1 = 0$), porous parameter ($\lambda_2 = 0$), Magnetic field parameter (M=0) and heat source (s = 0), but it increases in the presence of magnetic field parameter but the reverse effect is observed with an increase in the value of source parameter. Further, it is seen that an increase in magnitude of shrinking rate in the presence of both magnetic field parameter and heat source, Nu decreases. The Nusselt number remains positive in the presence of sink (s = -1). It is interesting to note that for an aqueous medium for higher value of Pr (Pr=7.0), the Nusselt number Nu assumes negative value.

It is to note that an increase in stretching rate and Prandtl number (Pr) both contribute to increase the rate of heat transfer but Pr contributes significantly. Moreover, in case of shrinking sheet high Prandtl number fluid causes a thermal instability at the surface (i.e. negative value of Nu) whereas no such case arises for stretching sheet.

Table 1 The rate of heat transfer $-0' (0)$ for different values of b/a.

b/a	Pr	M	S	Bhattacharyya [24]	G.C.Dash [18]	Present solution
-1.24	0.1	0	0	0.1282967	0.128166	0.118198
-1.24	0.5	0	0	0.0983723	0.0958855	0.095848
-1.24	0.5	1	-1	0.653725	0.59810371	0.674000
-1	0.71	0	0		0.228279813	0.228279
-1	0.71	1	0		0.324962755	0.324963
-1	0.71	1	0.2		0.178288797	0.178289
-0.5	0.71	1	0.2		0.299787756	0.299788
0	0.71	1	0.2		0.402840293	0.402840
1	0.71	1	0.2		0.574087826	0.574088
-1	7	1	0.2		-0.685148147	-0.685147

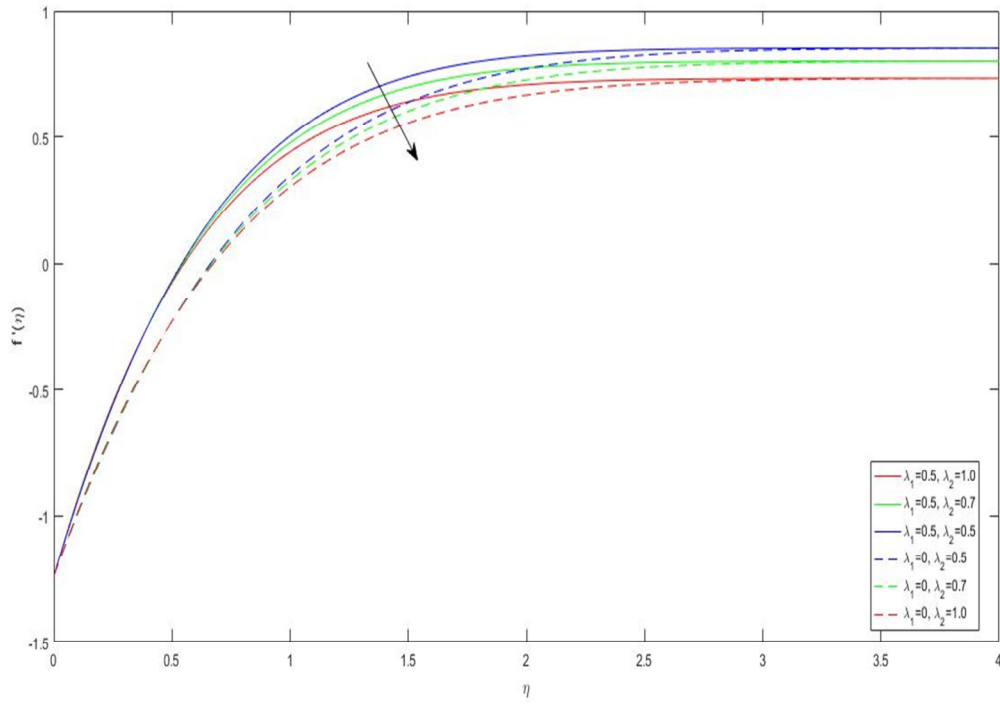


Figure 2. The velocity profile for shrinking sheet and different values of λ_2

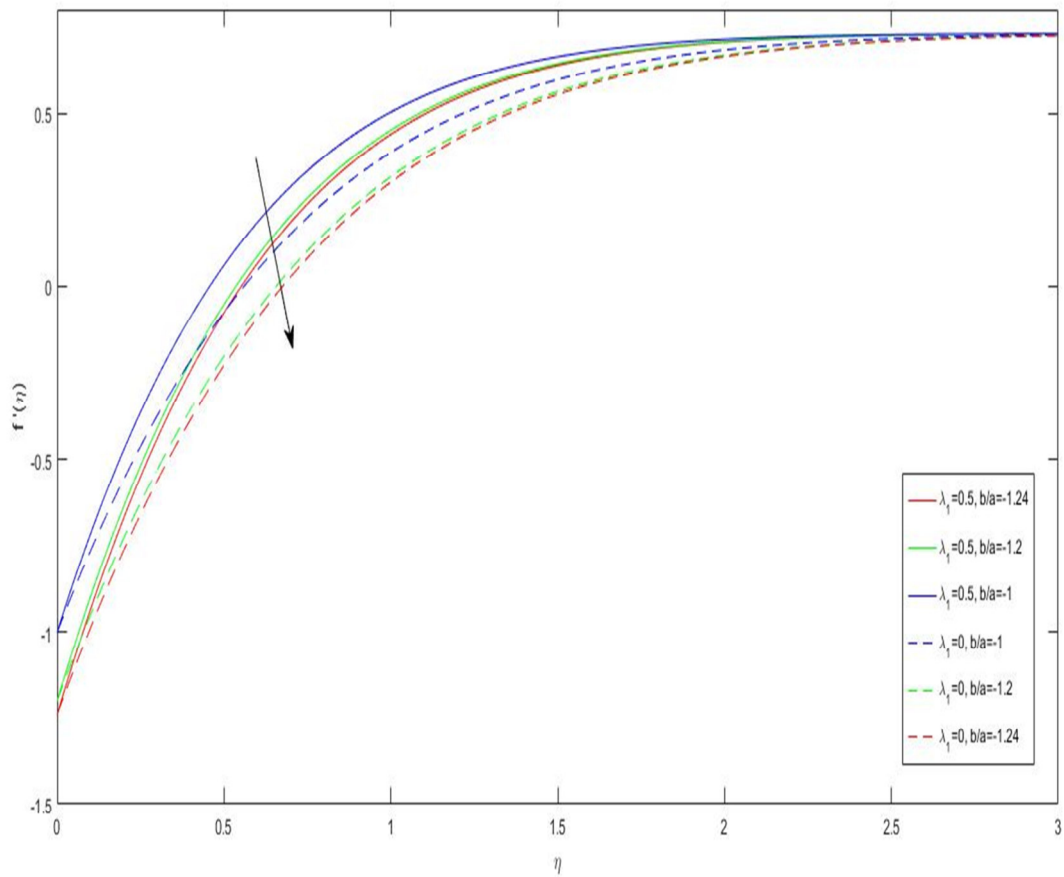


Figure 3. The velocity profile for different values of $\frac{b}{a}$

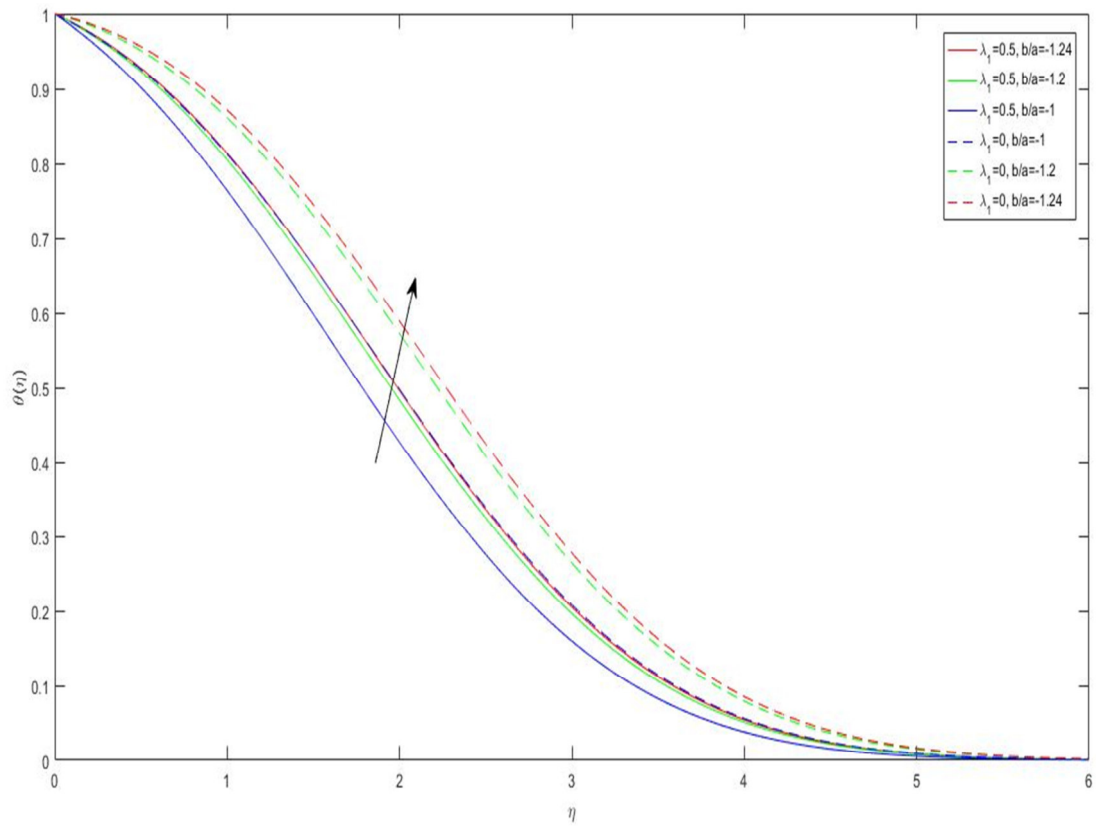


Figure 4. The temperature distribution for different values of b/a

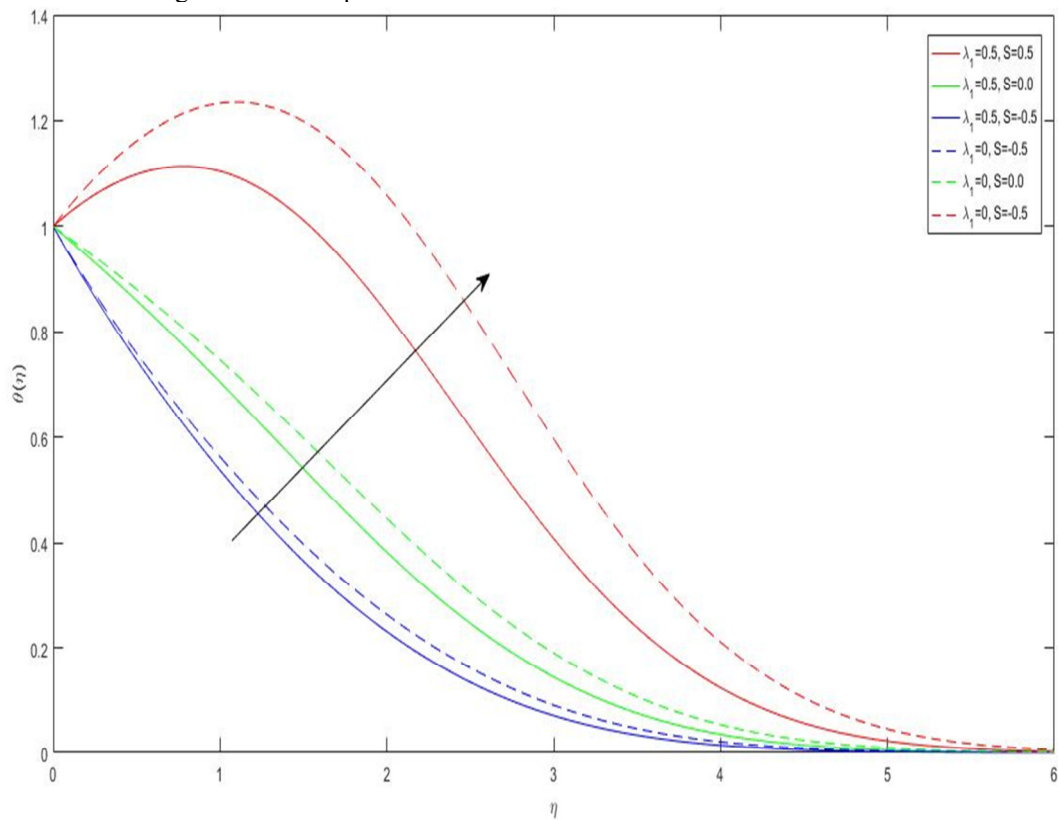


Figure 5. The variation of s on the temperature distribution

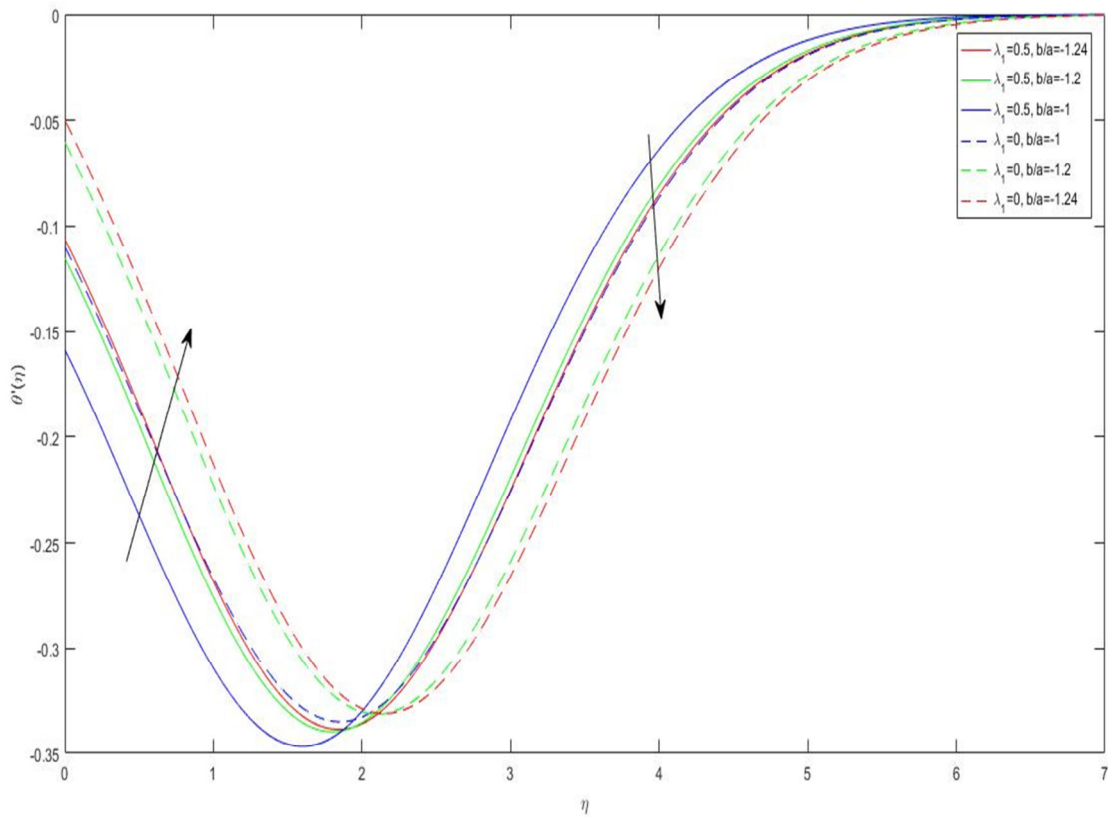


Figure 6. The variation of $\frac{b}{a}$ on temperature gradient

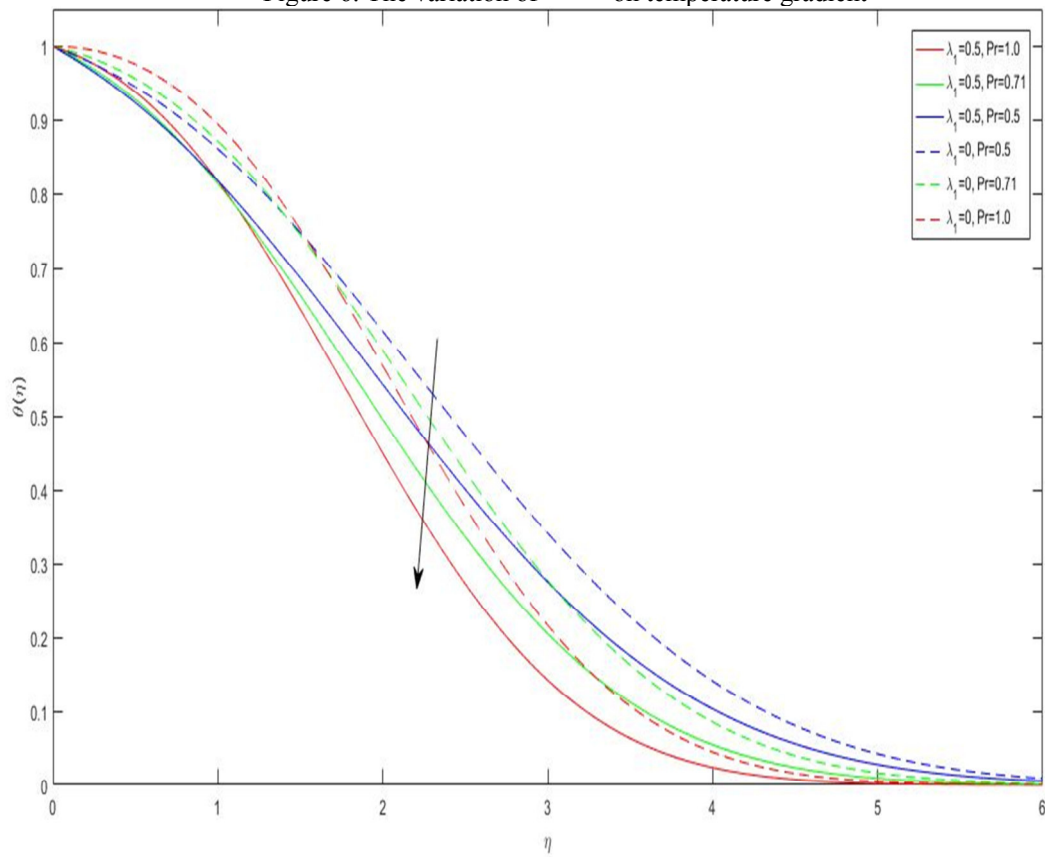


Figure 7. The temperature distribution for different values of Pr

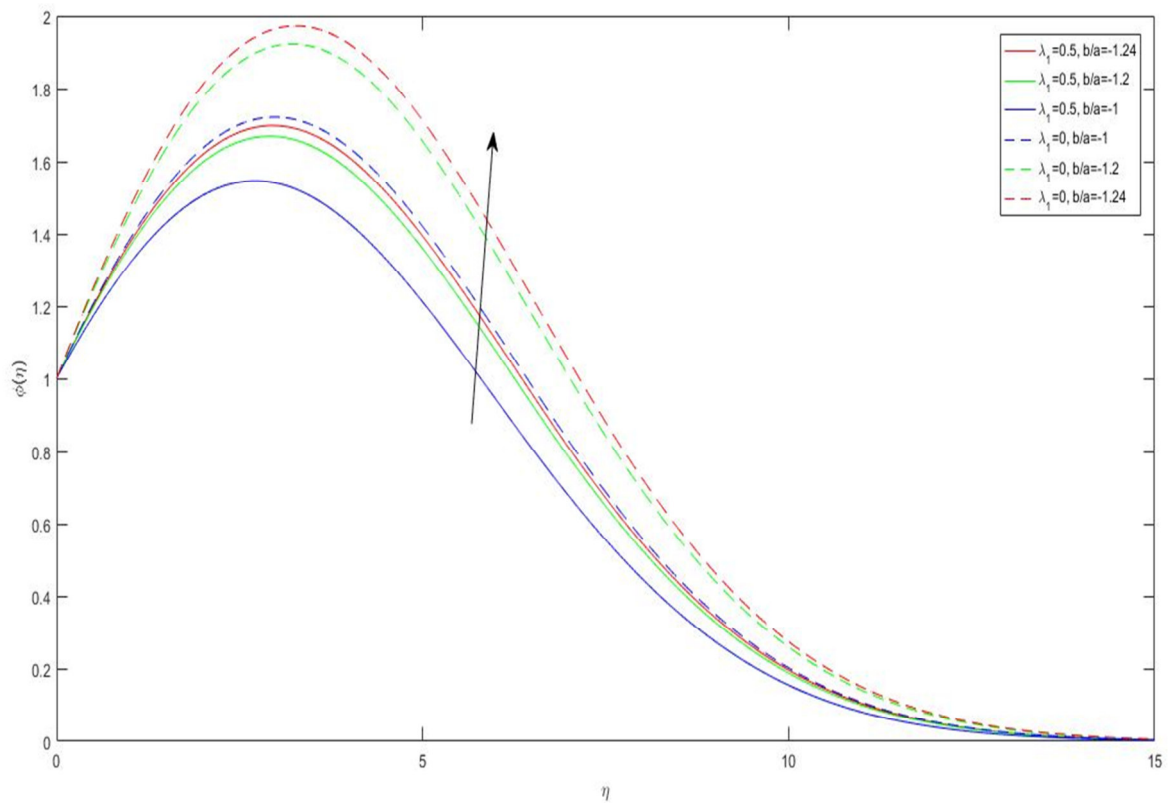


Figure 8. The variation of $\frac{b}{a}$ on concentration profile

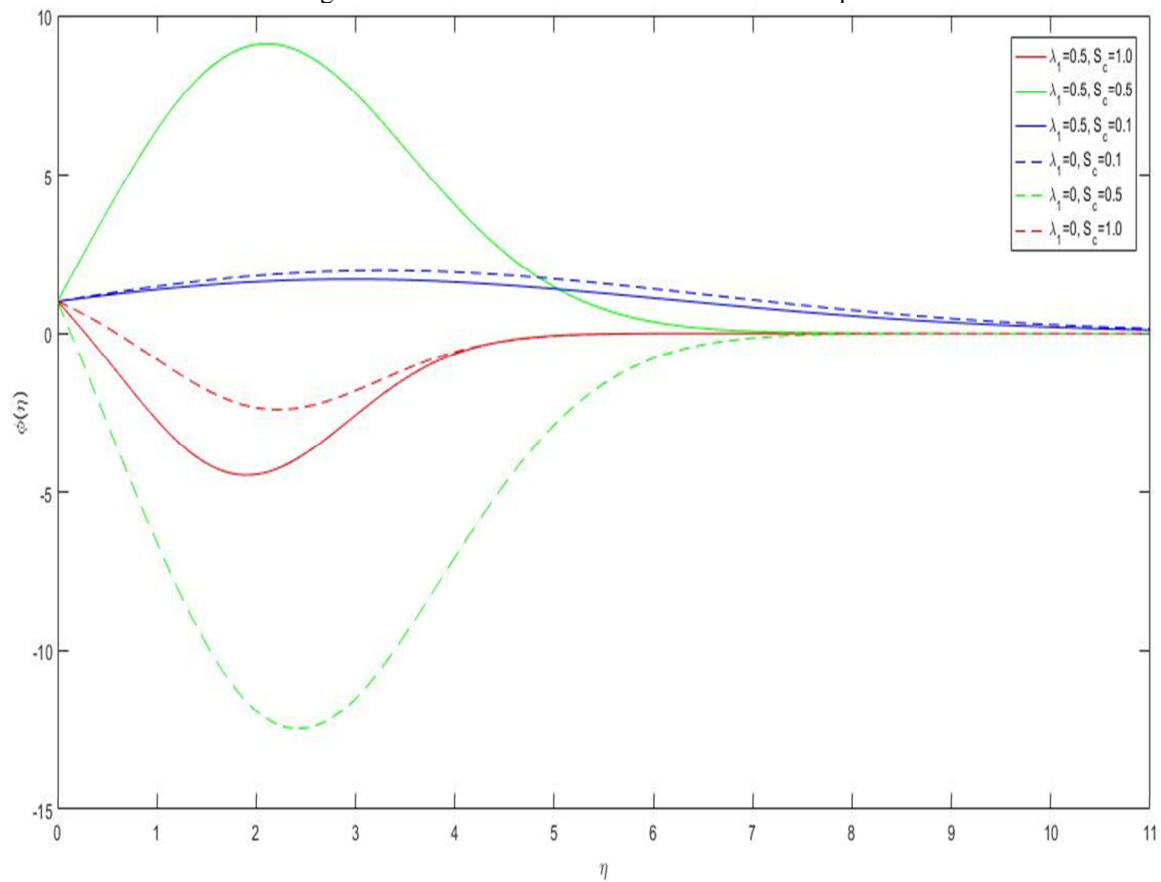


Figure 9. The variation of Sc on concentration profile

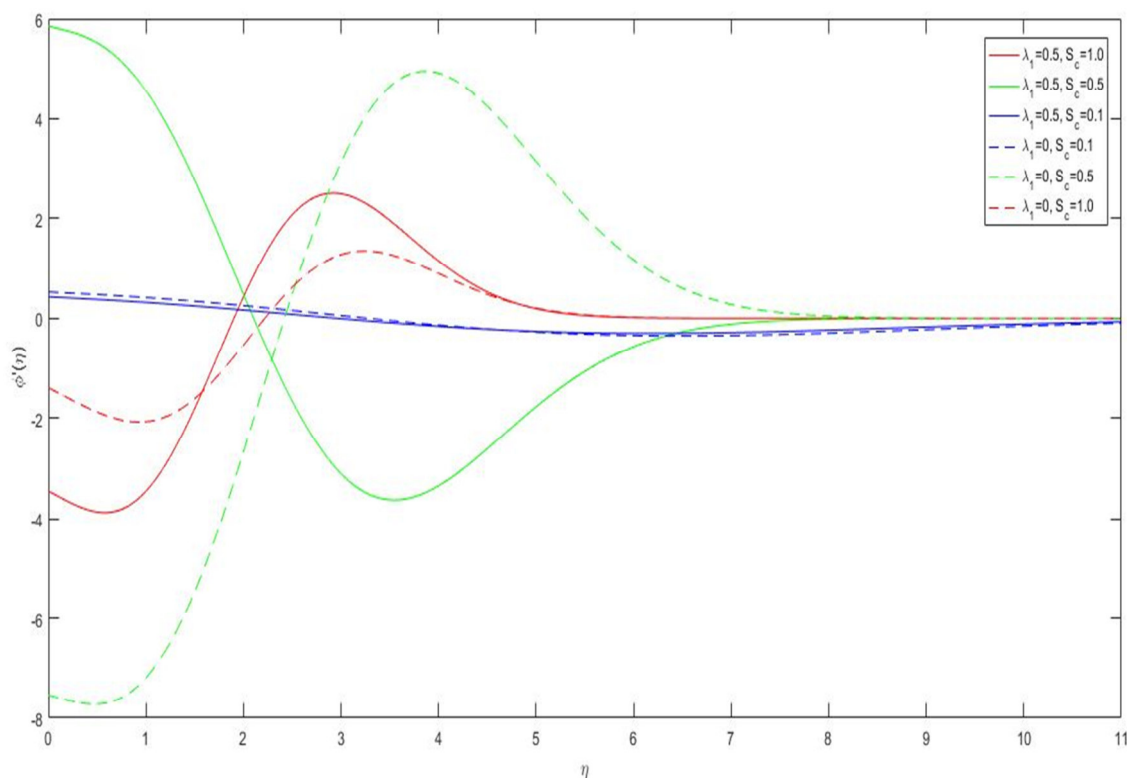


Figure 10. The variation of S_c on concentration gradient profile

REFERENCES:

1. B. C. Sakiadis, (1961). Boundary-layer behavior on continuous solid surfaces: I. Boundary-layer equations for two-dimensional and axisymmetric flow, *AIChE J.* 7, 26-28.
2. L. E. Erickson, L. T. Fan and V. G. Fox, (1966). Heat and Mass Transfer on a Moving Continuous Flat Plate with Suction and Injection, *Industrial & Engineering Chemistry Fundamentals*,5, 19-25.
3. L. J. Crane, (1970). Flow Past a Stretching Plate, *Z. Angew. Math. Phys.* 21, 645-647.
4. P. S. Gupta and A. S. Gupta, (1977). Heat and Mass Transfer on a Stretching Sheet with Suction or Blowing, *The Canadian Journal of Chemical Engineering*, 55, 744-746.
5. Wang, C.Y. (1984).The Three-Dimensional Flow Due to a Stretching Flat Surface. *Physics of Fluids*, 27, 1915-1917.
6. B.K. Dutta, P. Roy and A.S.Gupta, (1985). Temperature field in flow over a stretching surface with uniform heat flux, *International Communication in Heat Mass Transfer*, 12, 89-94.
7. Kartini Ahmad, Zahir Hanouf and Anuar Ishak, (2016). Mixed convection Jeffrey fluid flow over an exponentially stretching sheet with magnetohydrodynamic effect. *AIP Advances*, 6, 035024.
8. Maria Imtiaz, Tasawar Hayat, Ahmed Alsaedi, (2016). MHD Convective Flow of Jeffrey Fluid Due to a Curved Stretching Surface with Homogeneous Heterogeneous Reactions. *Journal Pone*, 11(9).
9. K.L. Krupa Lakshmi, B.J. Gireesha, Rama.S.R. Gorla, B. Mahanthesh, (2016). Effects of diffusion-thermo and thermo-diffusion on two-phase boundary layer flow past a stretching sheet with fluid-particle suspension and chemical reaction: A numerical study *Journal of the Nigerian Mathematical Society* 35, 66–81
10. Wang, C.Y., (2008). Stagnation Flow towards a Shrinking Sheet. *International Journal of Non-Linear Mechanics*, 43, 377-382.
11. Ishak, A., Nazar, R. and Pop, I. Mixed Convection on the Stagnation Point Flow toward a Vertical, Continuously Stretching Sheet. *Journal of Heat Transfer*, 129(2007), 1087-1090.
12. Ishak, A., Nazar, R. and Pop, I. Post Stagnation Point Boundary Layer Flow and Mixed Convection Heat Transfer over a Vertical, Linearly Stretching Sheet. *Archives of Mechanics*, 60(2008), 303-322.
13. Ishak, A., Jafar, K., Nazar, R. and Pop, I. MHD Stagnation Point Flow towards a Stretching Sheet. *Physica A: Statistical Mechanics and its Applications*, 388(2009), 3377-3383.
14. Chiam, T.C. Heat Transfer in a Fluid with Variable Thermal Conductivity over a Linearly Stretching Sheet. *Acta Mechanica*, 129(1998), 63-72.
15. Mahapatra, T.R. and Gupta, A.S. (2003) Stagnation Point Flow towards a Stretching Surface. *Canadian*

- Journal of Chemical Engineering*, 81(2003), 258-263.
16. I. S. Awaludin, P. D. Weidman and Anuar Ishak, (2016). Stability analysis of stagnation-point flow over a stretching/shrinking sheet, *AIP Advances* 6(4).
 17. Santosh chaudary and Mohan kumar choudhary, (2016). Heat and mass transfer by MHD flow near the stagnation point over a stretching /shrinking sheet in a porous medium. *Indian Journal of pure and Applied Physics*. 54, 209-217.
 18. G.C. Dash,R.S. Tripathy, M.M. Rashidi, S.R. Mishra, (2016). Numerical approach to boundary layer stagnation-point flow past a stretching/shrinking sheet., *Journal of Molecular Liquids*, 221, 860–866
 19. Mohamed Abd El-Aziz, (2016). Dual solutions in hydromagnetic stagnation point flow and heat transfer towards a stretching/shrinking sheet with non-uniform heat source/sink and variable surface heat flux, *Journal of the Egyptian Mathematical Society*, 24, 479–486
 20. Nor Azian Aini Mat, Norihan Md. Arifin, Roslinda Nazar, Norfifah Bachok, (2015). Boundary Layer Stagnation-Point Slip Flow and Heat Transfer towards a Shrinking/Stretching Cylinder over a Permeable Surface, *Applied Mathematics*, 6, 466-475.
 21. N.F. Fauzi , S. Ahmad , I. Pop, (2015). Stagnation point flow and heat transfer over a nonlinear shrinking sheet with slip effects. *Alexandria Engineering Journal*, 54, 929–934
 22. T.M. Agbaje, S. Mondal , Z.G. Makukula, S.S. Motsa, P. Sibanda, (2015). A new numerical approach to MHD stagnation point flow and heat transfer towards a stretching sheet. *Ain Shams Eng. J.* (paper accepted)
 23. Tasawar Hayat, Muhammad Waqas, Sabir Ali Shehzad, Ahmed Alsaedi J, (2015). MHD stagnation point flow of Jeffrey fluid by a radially stretching surface with viscous dissipation and Joule heating. *Hydrol. Hydromech.*, 63(4), 311–317.
 24. K. Bhattacharyya, (2011). Dual solution in boundary layer stagnation point flow and mass transfer with chemical reaction past a stretching/shrinking sheet, *Int. Commun. Heat Mass Transfer*, 38 917–922.
 25. M. Eswara Rao and S. Sreenadh, (2017). MHD Boundary Layer Flow of Jeffrey Fluid over a Stretching/Shrinking Sheet through Porous Medium, *Global Journal of Pure and Applied Mathematics*, 13, 3985-4001.
 26. N. Vishnu Ganesh, A.K Abdul Hakeem, B. Ganga, (2016). Darcy-Forchheimer flow of hydromagnetic nanofluid over a stretching/shrinking sheet in a thermally stratified porous medium with second order slip, viscous and Ohmic dissipations effects, *Ain Shams Eng. J.*(paper accepted)
 27. S. Baag, S.R. Mishra, G.C. Dash, M.R. Acharya, (2016). Entropy generation analysis for viscoelastic MHD flow over a stretching sheet embedded in a porous medium, *Ain Shams Engineering Journal*. (paper accepted)
 28. Hayat T, Awais M, Imtiaz A (2016). Heat Source/Sink in a Magneto-Hydrodynamic Non-Newtonian Fluid Flow in a Porous Medium: Dual Solutions. *PLOS ONE* 11(9) (2016).
 29. Vajravelu, K., S. Sreenadh, P. Lakshminarayana and G. Sucharitha (2016) Effect of heat transfer on the nonlinear peristaltic transport of a Jeffrey fluid through a finite vertical porous channel *International Journal of Biomathematics*, 9(02),1-24.
 30. Azhar Ali, H. Zaman, M. Z. Abidin, Naemullah, S. I. A. Shah, (2015). Analytic Solution for Fluid Flow over an Exponentially Stretching Porous Sheet with Surface Heat Flux in Porous Medium by Means of Homotopy Analysis Method, *American Journal of Computational Mathematics*, 5, 224-238.
 31. Ruchika Dhanai, Puneet Rana , Lokendra Kumar, (2015) Multiple solutions of MHD boundary layer flow and heat transfer behavior of nanofluids induced by a power-law stretching/shrinking permeable sheet with viscous dissipation, *Powder Technology* 273 62–70.